

1 **Investigating the influence of length-frequency data on the stock**
2 **assessment of Indian Ocean bigeye tuna**

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27

28 **Abstract**

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Most integrated stock assessment models are fit to alternative sources of data like indices of abundance and length/age composition of catches in specific fisheries. While indices of abundance are often standardized over time, not much attention is paid to the temporal stability of the length/age data. A sequential approach to fitting model outputs to all sources of data, varying the weight given to the length composition data, for Indian Ocean bigeye tuna (*Thunnus obesus*) is examined in this paper. The sensitivity of the bigeye tuna stock assessment to assumptions regarding the size-selectivity of key fisheries and the relative weight of size frequency data in the stock assessment is examined. Logistic, double normal, and cubic spline selectivity functions are used to model the size composition of catches in the main industrial fisheries (longline and purse seine). Overall, there is a poor fit of stock assessment models to the individual length frequency observations collected from these fisheries, although marginal improvements of fit were made when temporally variable selectivity was implemented in the SS-III framework using the above described functions. The most influential factor in the assessment was the weighting of the length composition data relative to the indices of stock abundance. Contradictory signals between these two data sources have a large effect on spawning biomass dynamics, and inference based on these weightings can produce different management conclusions. We examined alternative hypotheses and discuss the merits of fitting to all sources of data, or discounting some information if it has been unreliably collected over time. We emphasize that understanding the data is key to performing a well-calibrated stock assessment, and further refinements to the approach pursued here are discussed.

52 Introduction

53 Integrated stock assessment models have been used in fisheries management for the past three
54 decades (Fournier and Archibald 1982). However, blindly fitting models to all available sources of
55 data may lead to inaccurate results, as has been discussed extensively by Francis (2011). Often
56 fisheries change over time due to shifts in fishery selectivity or the catchability of different age or size
57 classes of fish. When this type of trend is apparent in the data, the modeller is faced with two choices:
58 1) model these as separate fisheries over time using different catchability estimates, or 2) model these
59 as one fishery with changing selectivity over time. Often the latter approach is used (Gavaris and
60 Ianelli 2002), as it easier to implement.

61

62 While most modellers and fisheries management practitioners understand the relative importance of
63 size selectivity and its interaction with biomass and effect on optimal yield and stock status (Haddon
64 2011, Hilborn and Walters 1992), it is an extremely difficult process to estimate (Hilborn and Walters
65 1992). Most assessments use external sources to justify the general shape of the selectivity curve (i.e.,
66 whether it is asymptotic or dome-shaped) and estimate the specific shape (i.e., the parameters of the
67 functional form) by fitting the model to age and/or length-composition data. In most tuna assessments
68 age data are limited, so length frequency data are the primary source of information. Tagging data can
69 also provide some information on selectivity, although in the case of the Indian Ocean region these
70 data are of limited use, primarily because tag mixing assumptions are violated (Langley et al. 2012).
71 In the case of a highly migratory species like bigeye tuna (*Thunnus obesus*; hereafter referred to as
72 BET), modellers assume similar functional forms for selectivity used by tuna Regional Fisheries
73 Management Organizations (RFMOs) across the globe. Note that estimated selectivity is not
74 independent of other parameters, particularly natural mortality (M), which is kept constant at different
75 ages through time ($M=0.8$ annually for the early ages in this assessment, and declines to $M=0.4$ by
76 age 3). These levels of natural mortality are comparable to those used by the Inter-American Tropical
77 Tuna Commission (IATTC) and Western Central Pacific Fisheries Commission (WCPFC) BET stock
78 assessments (Kolody et al. 2010).

79

80 Here we present a sequential analysis to account for temporal size-selective patterns in BET catch
81 data by modelling different functional forms of selectivity, along with temporal changes in selectivity
82 over time. The models examined use the following choices: 1) different selectivity functions are
83 examined for the main fisheries (longline and purse seine fisheries by area) to capture changes in
84 length frequencies over time, 2) different forms of temporal variability in size-selectivity are
85 examined, and 3) the influence of the effective sample size with and without time-varying selectivity
86 is examined. Although this analysis focuses on Indian Ocean bigeye tuna, the approach outlined here

87 would be useful in all stock assessments, and emphasizes that understanding the data and its
88 uncertainty is key to a rigorous and sound stock assessment.

89
90 BET accounts for 430K Mt (10% of all tropical tuna) of worldwide tuna catches by volume (2008-
91 2010, Herrera et al. *in press*) and is caught primarily in the Pacific Ocean (54%), followed by the
92 Indian (28%) and Atlantic Oceans (18%). The data used in this analysis are primarily from the
93 longline and purse seine fisheries in the Indian Ocean. The longline fishery (distant water)
94 commenced operation in the Indian Ocean during the early 1950s. BET represents a significant
95 component of the total catch from the longline fishery; catches reached a peak in the late 1990s-early
96 2000s at 70K to 90K Mt per annum. The purse seine fisheries (primarily log and FAD based fisheries)
97 and fresh-chilled longline fisheries developed in the mid-1980s and total BET catches peaked at
98 around 155K Mt in the late 1990s. Since the mid-2000s, the total annual BET catch has fallen
99 considerably, primarily due to a decline in the longline catch in the western equatorial region in
100 response to the threat of piracy off the Somali coast. In 2011 the total annual catch was estimated to
101 be around 91K Mt (Herrera et al. 2012). Small scale fisheries that encounter BET are the Maldivian
102 pole/line fishery and gillnet fisheries operating in the Indian Ocean. Both major fisheries have
103 collected extensive length frequency data over time and area, which are used in the model fitting
104 exercise described here.

105
106 Initial assessments of BET have generally applied non-equilibrium surplus production models
107 (Nishida and Rademeyer 2011) and integrated stock assessment methods that are fit to length
108 composition data, indices of abundance, and tagging data (Methot and Wetzel 2013, Kolody et al.
109 2010, Shono et al. 2009). Both assessment approaches indicate that the Indian Ocean BET stock has
110 not been overfished, although Kolody et al. (2010) highlighted the high level of uncertainty (both
111 derived parameter uncertainty and structural uncertainty, Punt and Hilborn 1997, Quinn 2003)
112 associated with key model parameters that resulted in a range of contrasting estimates of stock status,
113 some of which indicated that the stock is in an overfished state.

114
115 The approach pursued here builds on some of the structural uncertainty examined in Kolody et al.
116 (2010) and Langley et al. (2012). The main focus of this work is examining how different functional
117 forms of selectivity can affect stock assessment, and the impact of considering time-invariant vs.
118 temporally-variable selectivity. In addition, we examine the effect of differentially weighting size
119 composition data on model outcomes. If information from the fisheries suggests that the size
120 composition of the catch has changed in response to a change in fishery operations (for example, a
121 change in the spatial or seasonal operation of the fishery), it may be appropriate to estimate temporal
122 variation in the selectivity parameters as we demonstrate here. We examine some alternative
123 hypotheses regarding selectivity forms and weights used for fitting the length-composition data, and

124 the effect of these on reference points (or derived model outputs). The merits of fitting models to all
125 sources of data, or discounting some information if unreliably collected over time, are also discussed.

126 **Materials and Methods**

127 Construction and fitting of integrated stock assessment models combines all available data in a
128 statistical maximum likelihood estimation framework (Fournier and Archibald 1982; Maunder and
129 Punt 2013; Methot and Wetzel 2013). These models simultaneously estimate numerous parameters to
130 give the best fit to observed data (Deriso and Parma 1987, Fournier and Archibald 1982). For this
131 analysis we used the Stock Synthesis software (Methot 1989, Methot and Wetzel 2013) that adapts the
132 basic age-structured algorithms presented in Fournier and Archibald (1982). Stock Synthesis has
133 considerable flexibility in the parameterization of length- and age-based selectivity, including a range
134 of functional forms, formulation of priors for the main selectivity parameters, and temporal variability
135 (in blocks, as parameter deviates, or linked to an exogenous variable).

136

137 **Catch and Biological Data: Model Inputs**

138 **Temporal units**

139 Data were disaggregated by calendar quarter (quarter 1 = Jan-Mar), and the model was iterated on
140 quarterly time steps in order to capture potentially important seasonal dynamics over the period 1952-
141 2011. The model was aggregated by sex; age class bins were yearly with a plus group at age 10 (the
142 model worked on quarterly age increments resulting in 40 different quarterly ages in the model).

143

144 **Spatial structure, fishery dynamics, catch and CPUE data**

145 Spatial structure of population dynamics in a given fishery is an important consideration when
146 constructing a stock assessment model. BET population dynamics are spatially aggregated for the
147 purposes of these model runs; the main fisheries operating in three areas are shown in Table 1,
148 Figures 1 and 2. The primary fisheries modeled are longline in each of the three areas (LL 1-3), and
149 the Purse Seine Free School (PSFS) and Purse Seine Log School (PSLS) in Areas 1 and 2. Three other
150 fisheries with a shorter catch history are included: the fresh tuna fishery (LL in Area 2) a hook and
151 line fishery in Area 2, and a bait boat (BB) fishery in Area 1. The “other” category includes all other
152 catches, again in Areas 1 and 2, primarily the non-industrial fisheries.

153

154 Sampling coverage of the length frequencies of catches varies considerably by type of fishery
155 (multiple fleets make a fishery in one area; for example, the Japanese longline fleet is a subset of the
156 longline fishery), and by area. In the case of longline fisheries, sampling from log books for some
157 fleets can be as high as 80% (defined in terms of the number of fish sampled for length compared to
158 the number of fish recorded for catch and effort by vessels operating in the area). The purse seine

159 fleets report similar levels of coverage. However, in the case of the “other” fisheries the sampling
160 coverage is much lower, generally less than 5%, while bait boat coverage is in the range of 30%. The
161 sampling coverage of length-frequencies are high (greater than 30% of the total fish caught) for a
162 number of fleets (e.g., Taiwanese longline and European purse seine fleet), and low for other fleets
163 (less than 1%). Some investigators have noted inconsistencies over time in methods of collection of
164 length-frequency data for the longline fleet (Geehan et al. 2013).

165

166 Fishery catches are provided in Herrera et al. (2012). The main fisheries used in this analysis include
167 the LL fleets and the PS fleets which account for 90-95% of the catch (Figure 3). The length
168 composition data (Figure 3) for each fishery tended to be a composite of length data from a number of
169 different fleets, consisting of a mixture of commercial vessels, training vessels, and scientific
170 observers. Using aggregated fleet data may not capture differential operations in the individual fleets
171 (e.g., Japanese longline vessels compared to Taiwanese longline vessels). Japanese longline vessels
172 are the primary source of the length frequency data for BET in the early 1970s and 1980s, while in the
173 1990s Taiwan replaced Japan as the main longline fleet reporting size data. According to the
174 Overseas Fisheries Development Council (OFDC) of Taiwan, size measurements between 2000 and
175 2011 were recorded for over 4.4 million BET specimens from longline vessels. Between 2003 and
176 2005 alone – i.e., the years of highest sampling – length measurements were recorded for over 1.7
177 million BET samples by Taiwan. In addition to these differential fleet characteristics, the spatial
178 distribution of the operation of these fleets has also changed considerably over time

179

180 The primary abundance data used in the BET assessment models are taken from standardized CPUE
181 indices derived from the Japanese longline fleet, which has been in operation since the late 1950s.
182 This is the only such standardized data set collected systematically and, like other tuna RFMOs
183 around the world, we use it as a primary source of data in fitting these models. Standardized CPUE
184 indices for the entire Indian Ocean were derived from the Japanese longline fleet using a generalized
185 linear model (GLM, Satoh and Okamoto 2012, Hoyle and Okamoto 2011). The indices are derived by
186 year and quarter for 1960–2011 (Figure 4). The overall Indian Ocean CPUE indices are very similar
187 to the CPUE indices from the western equatorial region (Satoh and Okamoto 2012), and were all
188 assumed to have a coefficient of variation (CV) of 10%. The high level of precision was assumed
189 because the CPUE indices are the primary indicator of relative abundance in the assessment model
190 and so the derived trends in stock abundance should be generally consistent with these indices. For all
191 models examined in this analysis, catchability for the main longline fisheries was assumed to be
192 temporally invariant.

193

194 Given all these complexities, it seemed appropriate to use differential selectivity patterns by time and
195 fishery (stratified by area) to better capture some of the fishery-specific temporal and spatial

196 dynamics, as there is some evidence based on the 5 by 5 degree data (latitude and longitude degrees
197 on the Indian Ocean) that suggests that the magnitude of catch can vary by a factor of two across
198 different 5 by 5 degree areas over times (IOTC 2012).

199

200 **Model Structural Assumptions**

201 **Biological parameters**

202 Recent estimates of Indian Ocean BET growth derived from otolith and tag release/recovery studies
203 are available from Eveson et al. (2012). Growth estimates are available for both sexes combined. The
204 quarterly growth deviates from a von Bertalanffy growth function, with considerably lower growth for
205 quarterly age classes 4–8 (Figure 5). Maximum average length (L_{∞}) was estimated by Eveson et al.
206 (2012) at 150.9 cm fork length (FL). The growth model was unable to reliably estimate the standard
207 deviation of length-at-age; however, the most appropriate level of variation in length for all age
208 classes was considered to be represented by a coefficient of variation of 0.10 (P. Eveson, CSIRO
209 Marine Research, GPO Box 1538, Hobart, Tasmania 7001, Australia, pers. comm.). The growth
210 function was modelled in SS using age-specific deviates on the k growth parameter. Because this
211 feature has only recently been implemented in SS, it is currently not documented (R. Methot,
212 NWFSC, NOAA Fisheries, Seattle, WA 98112 USA pers. comm.) and is one of the first applications
213 within SS to use this feature (Figure 5).

214

215 The size at sexual maturity used in the model was equivalent to that applied by Shono et al. (2009)
216 and Kolody et al. (2010). Female fish were assumed to attain sexual maturity at 100 cm FL with full
217 sexual maturity at about 125 cm FL. The length-weight relationship was equivalent to that previously
218 used by Shono et al. (2009) and Kolody et al. (2010) and was originally derived by Nakamura and
219 Uchiyama (1966). Fish weight was determined using the allometric relationship, $a \text{ length}^b$, with $a =$
220 3.661×10^{-5} , and $b = 2.901$, where weight is in kilograms and length is in centimetres.

221

222 Age-specific natural mortality was equivalent to the schedule used by Shono et al. (2009) and Kolody
223 et al. (2010) where M is 0.8 annually for the early ages and declines to 0.4 by age 3 (quarterly
224 estimates of 0.2 and 0.1 were used in the model). The levels of natural mortality are comparable to
225 IATTC and WCPFC bigeye tuna stock assessments with relatively high natural mortality for the
226 younger age classes and natural mortality of about 0.1 per quarter for the adult age classes.

227

228 **Recruitment**

229 Recruitment occurs in each quarterly time step of the model. Recruitment was estimated as deviates
230 from the Beverton-Holt stock recruitment relationship (SRR), although deviates were estimated for
231 1964–2009 only (184 deviates). Recruitment deviates were not estimated for the earlier period of the

232 model due to the lack of longline CPUE indices prior to 1960 and the lack of length frequency data
 233 prior to 1965, and recruitment deviates were not estimated for the last eight quarters in the model as
 234 there is insufficient CPUE abundance index data to estimate recruitment in later years. Recruitment
 235 deviates are assumed to have a standard deviation (σ_R) of 0.6. The steepness (h) parameter of the SRR
 236 was fixed at a value of 0.8, an intermediate value from the range of values proposed by Harley (2011).

237

238 **Fishery dynamics and selectivity assumptions**

239 All selectivities were incorporated using the SS-III functionality (see Methot and Wetzel 2013) which
 240 can account for different forms of the selectivity function and aggregate fisheries into one form. For
 241 all fisheries, selectivity was estimated as an age-based process. Double normal selectivity was
 242 assumed for Areas 2 and 3 and logistic selectivity was assumed for Area 1 and the FL2 longline
 243 fishery. Selectivity is expressed as:

244

$$245 S_{y,f,l} = 1 + e^{(-\ln(19)(l-\beta_{1,y,f})/\beta_{2,y,f})^{-1}} \quad (\text{eq. 1})$$

246

247 where S is the proportion selected to the gear, y is the year, f is the fishery, and β_1 and β_2 are
 248 parameters related to the size at which 50% (β_1) selectivity occurs for fishery f in year y . β_2 is the
 249 difference between the size at 95% selectivity and 50% selectivity for the same fishery and year
 250 (Methot 2009).

251

252 The selectivities of the LL2, LL3, PSLS and BB fisheries were estimated using a double normal
 253 functional form to account for the bimodal length composition of the catch from the PSFS fishery, and
 254 the selectivity was modelled using a cubic spline with 6 nodes (Haerdle 1990). Limited data were
 255 available to estimate the selectivity of either the PSLS2 or PSFS2 fisheries (i.e., purse seine fisheries
 256 operating in Area 2). The selectivity of these fisheries was constrained to be equivalent to the
 257 corresponding fishery selectivity in the western region. Selectivity in this case was calculated as:

258

$$259 S_{y,f,l} = asc_{y,f,l}(1 - j_{1,y,f,l}) + j_{1,y,f,l} \left((1 - j_{2,y,f,l}) + j_{2,y,f,l} dsc_{y,f,l} \right) \quad (\text{eq.2})$$

260

261 where asc and dsc are the ascending and descending functions of the normal and are described by the
 262 joiner functions, $j_{1,y,f,l}$, and $j_{2,y,f,l}$ respectively (for more details see Methot 2009). Five parameters
 263 are used to estimate this function and non-informative normal priors are used to bound the parameter
 264 estimates. Note that both eq. 1 and 2 could be sex-specific but are not in this case.

265

266 Limited size data are available from the “other” fisheries. Initial attempts to estimate independent
 267 selectivities for these fisheries were not successful, partly due to the variability in length composition

268 among samples. In aggregate, the length compositions are bimodal and similar to the length
269 composition from the PSFS fishery. On that basis, the selectivities for the two “other” fisheries (OT1
270 and OT2) were assumed to be equivalent to the PSFS fishery. Similarly, limited length data are
271 available for the mixed gears (hand-line, gillnet/longline combination) fishery in Area 2 (LINE2,
272 Table 1), so the selectivity was assumed to be equivalent to the main longline fishery. Finally, for the
273 single region model, the CPUE indices are linked to the selectivity of the LL1 fishery.

274
275
276

Selectivity Sensitivity Model Runs

277 A range of models was configured to investigate how selectivity affects the assessment (see Table 2
278 for more details). The following models were examined:

- 279 1) The base case (Scenario 1) model uses a logistic selectivity in Area 1 for the longline fishery
280 and fresh tuna longline fishery. Double normal selectivity functions were used for the
281 longline fisheries in Area 2 and Area 3, and the PSLS in Areas 1 and 2. This function was
282 applied to the BB fishery as well. Finally the PSFS used a cubic spline function. The other
283 categories were modeled with the same cubic spline function, as some of the catches appeared
284 to have the same bimodal functionality as the PSFS. A model run with a larger effective
285 sample size for the length composition data from the LL and PS fisheries was conducted as
286 well (Scenario 5).
- 287 2) In scenario 2 and 6, the only change from the Scenario 1 parameterization was that logistic
288 functions were assessed for all longline fisheries, to contrast with the base model which
289 parameterized the selectivity of LL 2 and 3 using the double normal functional form.
- 290 3) In scenarios 3 and 7, selectivity was varied over time in three discrete time blocks (1952-
291 1972, 1972-2001, and 2002-2011) to capture some of the changes in size composition
292 observed in the LL fisheries over time (see Figure 8, where some evidence is suggested for
293 changes in the 1970s and then again in the 2000s, Scenarios 3 and 7). The logistic selectivity
294 function was still used in Area 1 for the longline fishery and fresh tuna longline fishery, and
295 the double normal selectivity functions were used for the longline fisheries in Area 2 and
296 Area 3, but time period blocks were used instead of the time-invariant approaches used in
297 Scenario 1 and 5. This approach would translate into three different selectivities for the LL
298 fishery by area and time (a total of 9 fisheries, though Area 2 LL and Area 3 LL share
299 parameters; Scenarios 3 and 7 use these forms and only change the LL selectivity by time
300 using).
- 301 4) Scenarios 4 and 8 used time varying selectivity for both the LL and PS fisheries by time and
302 area for the LL and PSLS fisheries (3 different selectivities for the LL fishery by area and
303 time make a total of 9 fisheries, though Area 2 LL and Area 3 LL share parameters, and 3
304 selectivities for PSLS for a grand total of 12 new fisheries as Area 1 and Area 2 share the

305 same selectivity function). Note that scenario 4 and 8 analyze the LL and PSLs
306 simultaneously.

307 5) We also constructed a simple model aggregating all gear-specific fisheries operating in
308 multiple areas into one fishery across the entire Indian Ocean; a total of four fisheries was
309 included in this analysis (LL, PSFS, PSLs and “other”). Cubic spline functions were used for
310 the selectivities, including LL (scenario 9). This model only used recruitment deviates from
311 the period 1985-2007, and operated on an annual time step with seasons (at this resolution this
312 is 22 recruitment deviates), while the other models operated on a quarterly time step and
313 estimated deviates for 46 years (at a quarterly resolution this is 184 recruitment deviates).

314

315 We examined the effect of weighting the length composition data heavily versus discounting these
316 data by contrasting scenarios 1-4 with scenarios 4-8. An effective sample size of 10 was used across
317 all fisheries in the case of the base run, and an effective sample size of 100 for the LL and PS fisheries
318 was used for weighting the length composition data more heavily (Scenarios 5-9). For the “other”
319 fisheries an ESS of 10 was applied for all scenarios. In all the scenarios examined, the CV for the
320 index of abundance was held constant at 0.1. We compare the MLE estimates of current biomass
321 versus initial biomass over time to demonstrate how these alternative assumptions affect selectivity.

322

323 **Likelihood profile Analysis**

324 Profile likelihood (Edwards 1992) techniques were used to examine the effect of one parameter,
325 recruitment at virgin biomass levels (R_0), and its interaction with selectivity on the overall model fit
326 using the base case scenario as this is informative since M and growth are fixed. Since selectivity is
327 tightly constrained by the LL1 logistic function, different estimates of R_0 will reflect the fishing
328 mortality and temporal trends in recruitment from the two main data sets examined in this paper.

329

330 **Results**

331 For the aggregated fishery (Table 3, Scenario 9), fits to the aggregated length composition data (over
332 all time periods for a single fishery) were reasonable while the fits to individual length observations
333 were very poor, thus this model was disregarded as it failed to account for the length frequencies
334 observed in any of the fisheries over time.

335

336 The base model (Scenario 1) exhibits a relatively good fit to the abundance indices (Figure 6a; Table
337 2, Scenario 1), and a reasonable fit to the length composition data aggregated over time for the main
338 fisheries (Figure 6b; Table 2, Scenario 1). While the average trend is captured reasonably well in the
339 main fisheries, i.e., the longline and purse seine fisheries, the temporal variation is not captured as
340 well (Figure 9). Figure 9 displays the Pearson's residuals where the circles are positive (dark) or
341 negative (light) residuals between the model estimates of length composition and the observed length

342 frequency of the catch in the particular fishery and area. The fits are poor although typical for longline
343 size data, with serious structural change problems through time (Figure 9, Table 2). The time-varying
344 selectivity has very little visible effect on the residual pattern (Figure 9, Table 2).

345

346 Table 2 lists diagnostics measuring the goodness of fit, namely the negative log-likelihood values of
347 the different components of the model, the length frequency component and the survey component
348 (the catch component is left out as it is often negligible in these models). Note that the model of the
349 four aggregated fisheries (Scenario 9 in Table 2 which had 52 parameters) is not comparable to the
350 other models presented (Table 2) unless we use other statistics like AIC (Akaike 1983), though we do
351 report reference points obtained from the aggregated model (Table 3, scenario 9).

352

353 In the case of using the logistic versus the double normal functions for the LL fishery in Areas 2 and 3
354 (Figure 7), the fits were comparable (Table 2, Scenario 2) though the base model fit is better than the
355 logistic fit (Table 2) based on the overall likelihood values. While the logistic function may not result
356 in as good a fit as the double normal function, it also has fewer parameters to estimate. In addition, the
357 logistic function does not have any problems with denoting a cryptic biomass as all age classes are
358 fully vulnerable after a certain age. This is not the case with a dome-shaped selectivity curve like the
359 double normal curve. In our case, this is not a problem as there is still one fishery with logistic
360 selectivity within the model domain. While the logistic function fits the data because full selectivity
361 occurs at a much younger age, the double normal function achieves this fit by including fewer older
362 fish in the catch.

363

364 Due to variation in the length composition data over time (Figure 8) among fleets, using temporally
365 variable selectivity with a higher weight on length frequency data gave marginally better fits for many
366 fisheries (Figure 9) but may have resulted in poorer fits for some fisheries (PSLS1). The fits compare
367 models with lower effective sample size, i.e. in this case the base model with lower effective sample
368 size, and the time varying selectivity models with lower effective sample size (Scenario 1 and 4
369 respectively). This was done so we could take the confounding effect of effective sample size out of
370 the time varying selectivity component. A similar exercise was conducted for models with higher
371 effective sample size, but the results showed similar trends as we have here.

372

373 In essence the overall shape of the selectivity curve does not change much over time (Figure 10),
374 though the LL fishery appears to be selecting older fish over time. This pattern does not change when
375 heavier weight is given to size-selectivity data. Note, however that if these data were weighted with a
376 large effective sample size, it would have a large impact on the overall assessment. Even though the
377 temporally-variable component was added in block format, the residual patterns still remain quite
378 similar (Figure 9). The only noticeable change is that the magnitude of the residuals decreases when

379 the time varying component is added for the LL fishery in the 1970s and after 2003, when different
380 selectivity blocks are introduced in the fitting procedure. It could be concluded that the time varying
381 selectivity blocks are not adequate to account for the variation in size over time and the apparent
382 inconsistency between the length-frequency data and the index of abundance.

383

384 To examine the influence of the different sets of length-composition data on the estimation of
385 recruitment at virgin biomass levels R_0 , we conducted a likelihood profile analysis. Since M and
386 growth are fixed and selectivity tightly constrained by the LL1 logistic function, different estimates of
387 R_0 will reflect the fishing mortality and temporal trends in recruitment from the two main data sets. It
388 is evident from the likelihood profiles that there is somewhat conflicting information about R_0 from
389 the two data sets, with the overall length data indicating lower overall stock size (Figure 11). Further
390 examination indicates that the longline and fresh tuna longline fisheries in these areas (primarily in
391 Areas 1 and 2, figure not shown) are having the largest influence on the R_0 parameter, primarily
392 because there are few older fish in the populations. Any biases in these length frequencies, mis-
393 specification of the selectivity curve, or use of incorrect M , can have huge effects on the assessment
394 (Figure 11) as is evident with the estimates of target reference points S_{MSY} and Yield (Table 3, Figure
395 12).

396

397 A comparison of the different sets of models with similar effective sample size weightings (Table 2)
398 shows marginal improvements in the overall log-likelihood values for models with the same effective
399 sample size (sensitivity 1 to 4 and sensitivity 5 to 8 respectively). The log-likelihood values from
400 models with different effective sample size weightings cannot be directly compared, but these
401 diagnostics can be used in a qualitative manner to assess how the fits may be improving (accounting
402 for the differences in parameters estimated) for cases with the same effective sample size for the
403 length frequency data. A large effect on the assessment dynamics (Figure 12) is observed by
404 weighting the length composition data higher (assigning a sensitivity of 5 versus 1). Adding
405 temporally-variable selectivity (Table 2, sensitivity 3, 4 or sensitivity 7, 8) or different functional
406 forms (Table 2, sensitivity 2 or sensitivity 6), resulting in a marginal improvement in fit to the length
407 frequency data, has minor effects on management parameters obtained from the assessment (for
408 scenarios with the same effective sample size for the length frequency data).

409

410 Finally, when we contrasted the model runs with higher and lower effective sample sizes (Figure 13)
411 and examined how this weighting relates to the fits to the different datasets used in the model, we
412 found contradictory signals between the index of abundance and the length frequency data. While in
413 the analysis presented here, the effect of these different formulations on the assessment is negligible
414 in terms of the current stock status, this effect may not be negligible in other global assessments. All
415 scenarios investigated indicate that the current stock size (B_{2011}) is greater than B_{MSY} (low effective

416 sample size scenarios; between 1.3-2.3), and current fishing mortality rates are below F_{MSY} .
417 Weighting the length-composition data more heavily produces a more pessimistic picture of the stock,
418 i.e., B_{2011}/B_{MSY} is between 1.14 and 1.94, and F_{2011}/F_{MSY} is between 0.41 and 0.66 for all combinations
419 examined. Consequentially target optimal yields are 160-270 kT from the lower effective sample size
420 combinations versus 93kT -115 kT from the higher effective sample size combinations.

421 **Discussion**

422 Francis (2011) suggests that in cases where there are contradictory signals between the length-
423 composition data and the index of abundance, it is almost always more important to capture the index
424 of abundance over the length composition data. Fitting to the length-composition rather than the
425 abundance data may be misleading, as this approach gives more weight to processes of which we have
426 a poor understanding, and which are also correlated with the overall abundance signal (Francis 2011).
427 In most integrated models used across the globe, it is the nature of the modeler/scientist to use all the
428 data. However, as shown in this case, it is extremely important to understand the data before they are
429 used in the assessment. If the length frequency data are incorrect, then the resulting model will be
430 biased, and management advice resulting from the model will be incorrect as well.

431
432 This paper illustrates a sequential approach on how to model selectivity, the potential impacts of
433 different selectivity assumptions, and effects of these assumptions on stock assessment outputs. Three
434 different critical issues for analysing selectivity are illustrated here: 1) the form of the curve, 2)
435 temporally-variable selectivity and its appropriate use, and 3) the effective sample size of the length-
436 composition data that affects the estimation of key parameters in the assessment and in turn their
437 effect on derived parameters from the assessment. While most of the results were similar when
438 comparing changes in selectivity assumptions, the analysis highlights the importance of weighting the
439 length-composition data. The weighting issue is also related to fishing mortality assumed in the
440 assessment, and recruitment deviation estimated in the model, but this question is not examined here
441 extensively.

442
443 While developing the models here, a simpler approach was initially taken (Table 1, Scenario 9).
444 However, this model was abandoned as it did not capture changes in length composition over time.
445 This outcome was not surprising as the fisheries were aggregated, and using a cubic spline function
446 for selectivity, while allowing flexibility that captures bimodal length frequencies, still fails to account
447 for all the complexities in the temporal dynamics of the fishery. Thus, keeping the fisheries at least
448 separated geographically may more accurately reflect fishery dynamics, provided the data are
449 unbiased and consistently sampled over time, and so this approach was used in subsequent model runs
450 (Crone et al. this edition).

451

452 Shape of the Selectivity Curve Used and its Effects

453 We conclude from our analyses that while the shape of the selectivity function is important in these
454 fisheries, it does not have a significant effect on either the fits to the length-composition data or to the
455 abundance index data, unless it is weighted heavily. Our model run outputs are likely too variable
456 between time steps and among fisheries to reliably fit the contradictory signals, and the estimated
457 selectivity simply reflects the average pattern of fishery exploitation. While a possible improvement
458 may be to fit the length-composition data using selectivity deviates for each time step, that approach
459 might be tantamount to fitting the model to the error in the observations. The use of a logistic function
460 vs. a double normal function has only marginal effects on the overall results, unless we impose a
461 larger effective sample size on the data (Table 3, Figure 7) which forces the model to fit to the length-
462 frequency component. Even then the shape does not differ substantially as is evident in Figure 10.

463

464 The issue of whether we use temporally variable selectivity is intricately confounded by the length-
465 frequency data sampled. It is highly unlikely that the fisheries, particularly the sizes targeted, have
466 remained unchanged in the last 50 years, therefore using time-invariant selectivity will probably bias
467 our estimates. However, as is demonstrated here, if the length-composition data are inconsistently
468 measured over time (Figure 14), then putting unduly heavy weight on this parameter can also bias the
469 assessment. Finally, adding temporally variable selectivity gives an overly optimistic picture of the
470 stock status in the case when we don't weight the length composition data (Figure 13, Scenario 3 and
471 4; Table 3), and a pessimistic view of the stock in the case where the length-composition data are
472 weighted heavily (Figure 13, Scenario 7 and 8, Table 3). In our analysis we chose to put a lower
473 weight on the length composition data rather than give undue weight to the length composition data
474 based on criteria stated in Francis (2011). As a result of this approach we estimate different levels of
475 biomass than if we chose to weight the length-composition data higher (Figure 13). This discrepancy
476 occurs primarily because the length frequency data from the longline and fresh tuna fishery in Areas 1
477 and 2 are highly influential in the model. Since natural mortality (M) and growth are fixed, and
478 selectivity tightly constrained by either the logistic or double normal function, a different R0 and
479 recruitment deviates are estimated to better fit to the length observations. Hence we observe the lower
480 R0 values, an increase in recruitment in the 1970s, and increases in recruitment in the 2000s.

481

482 The modeled biomass trajectories resulting from the different combinations of input data (Figure 13)
483 have different outcomes as far as management advice is concerned. The issue with the estimated
484 selectivity curves (Figure 7 and Figure 10) that indicate a sharp decline in stock at around age 7 is
485 common when using the double normal function as this approach can cause convergence issues. This
486 problem typically occurs as the growth curve flattens off by age 7 (Figure 5). In addition, we see very
487 few fish over this size in the length composition data (Figure 8), causing these curves to exhibit the

488 declining limb, which would mean we still have a large number of older fish in the population (M
489 values used imply enough older fish available in the population).

490

491 **Data Issues Related to Estimated Length Compositions and Selectivity**

492 It is evident that either changes are occurring in the fishery over time (Figure 8 and Figure 15), or
493 there are problems with the sampling coverage after the year 2000. It is more likely that something
494 changed in the sampling regime after 2000 (Geehan et al. 2013). Further examination of the data
495 (Figures 14 and 15) indicates that the sampling coverage from the main longline fisheries has changed
496 during the period examined. In the 1970s and 1980s the main source of information for the length
497 frequency data (Figure 14b) was the Japanese longline fleet. However, in recent years these data have
498 been almost entirely contributed by Taiwan (Figure 14a). In addition the Taiwanese data collection
499 techniques and systems changed in the late 1990s (Chang and Wang 1998, Dr. S. Wang personal
500 comm.). Based on the sampling data it appears that larger fish are now encountered in larger
501 proportions than prior to the 2000s, and the overall variance in length-composition in the catch data
502 has also decreased. These observations indicate that there are inconsistencies in the length
503 composition data over time, thus the data series may not be entirely reliable. Because close to 90% of
504 the overall catch comes from these fleets, bias in these data has a large effect on the results of the
505 overall assessment.

506

507 Based on these observations, two alternative hypothesis may be proposed: 1) the length frequency
508 data are reliable and the stock is much less abundant than previously estimated (Table 3, Figure 13),
509 or 2) the stock is somewhat more abundant, the abundance index data are more reliable, and the length
510 frequency data are not as reliable (Figure 13, Table 3). A third alternative could also be examined
511 (though not in this paper): the data are reliable until the early 2000s when the sampling regime
512 changed. Under this scenario, we could fit the model to the length-frequency data until 2000, and then
513 only to the abundance index data after that. However, an examination of the earlier fits to the length
514 frequency data prior to 2000 (Figure 9, base case) still reveals a poor fit to the length-frequency
515 samples in those years. Another alternative would be to fix selectivity at the values estimated through
516 the logistic or double normal functions and then fit to the abundance data iteratively (Iwata et al. this
517 edition). This approach would ensure that we accounted for the catch being taken out at the right size
518 and fit to the overall abundance, without worrying about fitting to the length-frequency component as
519 well.

520

521 In deciding between alternatives (1), and (2) stated above, Francis (2011) suggests weighting the
522 index data more than the length composition data (which we do, Table 2, Figure 12). Until we have a
523 thorough understanding of the length composition data used in tuning these models, we are forced to
524 rely on the index of abundance data that is compiled and analyzed by the LL fleets of Japan. More

525 effort may also be required to understand why the index of abundance jumped in the mid-1970s.
526 Bigelow et al. (2002) suggest that fleet targeting could be the reason for this increase, meaning that
527 the gear was set at a different depth specifically to catch BET. Alternative standardization procedures
528 using different depths of fishing as a covariate, and the correct assigning of species compositions
529 (these were problematic prior to the 1970s, Herrera et al. 2012) during that period could provide
530 alternative indices of abundance (Bigelow et al. 2002). However, since this approach would require a
531 thorough re-examination of the operational data, it is beyond the scope of this study.

532

533 **Management Implications of Selectivity and Weighting of Data**

534 While size-selectivity is extremely important and directly related to estimates of optimal yield, target
535 spawning stock sizes, and overall fishing mortality (F), the results from this study indicate that the
536 functional forms have little effect after the majority of the fish become mature. Whether we use a
537 logistic or double normal function (declining limb of selectivity) the overall effect is marginal, other
538 than when we use temporally variable selectivity with lower weights on the length composition data,
539 where the reference points and yields are significantly higher than the other scenarios (Figure 13,
540 Table 3). For convergence issues, one needs at least one asymptotic form, which we used in LL 1. As
541 Wang et al. (this edition) show, the functional form of the selectivity (in their case asymptotic) could
542 cause biases as it is confounded with the maximum length and the observed length-compositions
543 observed in the fishery. While temporally variable selectivity fits the length-composition data better,
544 if the length composition is weighed higher, it has a large effect on R0 (Figure 11) and the overall
545 spawning stock biomass trajectories (Figure 13), indicating a declining recruitment trend and possibly
546 lower optimal spawning stock sizes. The model formulations with the logistic function also estimate a
547 larger fishing mortality rate compared to models with a declining limb in selectivity for obvious
548 reasons.

549

550 **Further Improvements in Model Formulations of Selectivity**

551 Further refinement of the fisheries by area and jurisdiction could provide the model with more
552 consistent data for length frequencies and indices of abundance. In addition, a length frequency data
553 set that accounts for changes in targeting could also improve the fit of the model, as the stock could be
554 modeled as separate fisheries based on when these targeting changes occurred. If selectivity of the
555 fleets has changed over time (which is likely), using the temporally-variable component makes sense.
556 However, if there is no drastic change in the length-composition data, and we use the same functional
557 form, we get very slight differences in these curves as seen in Figures 7 and 10. Modeling these as
558 entirely different fisheries, with different functional forms (double normal versus logistic), could
559 possibly produce improvements in the assessment, provided we have some external source of
560 information indicating that these fisheries operated very differently in these two periods.

561

562 Alternative model assumptions such as considering the appropriateness of age- vs. length-based
563 selectivity should also be undertaken (though an analysis to look at these effects, not presented here,
564 gave very similar results). It is also important to consider reliability of other key fixed model
565 parameters, especially growth and M-at-age, which have a large impact on selectivity and available
566 biomass at any given time. Other key processes that may be affecting this assessment are regional
567 stock structure and spatial differences in recruitment processes; these should be examined along with
568 the selectivity assumptions presented here.

569

570 Finally, the use of iterative reweighting approaches as suggested by Iwata et al. (this edition) is
571 another alternative to improving the selectivity and not fitting to the catch so that we can take the
572 catch out at the appropriate age without fitting to the length-composition data. This approach may not
573 be helpful if sampling is indeed biased, as is plausible in this case (Figure 15), as the mean length of
574 the catch appears to increase over time while the variability decreases over time (kurtosis decreases).
575 However, one of our key conclusions is that it is critical to first understand whether the changes in
576 length-frequencies are real or biased. This is a critical step, given the importance of these data in
577 influencing the overall assessment results.

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581

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657 function and its influence on management advice. *Fisheries Research this edition*.

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711 size of the green proportional circles indicates the sampling coverage in each year, which are scaled relative to
712 the minimum sampling coverage of one fish per tonne of catch recommended by the Indian Ocean Tuna
713 Commission (denoted by the black circle at the centre of each proportional circle). Years with proportional
714 circles larger than the minimum sampling standard indicate relatively high sampling coverage in a given year;
715 the larger the circle the higher the sampling coverage. The crosshairs indicate the average length of sampled
716 cohorts in each year class.

717

718

719

720 **Table 1. Definitions of the individual model fisheries**
721

Code	Method	Region
FL2	Longline, fresh tuna fisheries	2
LL1	Longline, distant water	1
LL2	Longline, distant water	2
LL3	Longline, distant water	3
PSFS1	Purse seine, free school	1
PSFS2	Purse seine, free school	2
PSLS1	Purse seine, associated sets	1
PSLS2	Purse seine, associated sets	2
BB1	Baitboat and small scale encircling gears (PSS, RN)	1
LINE2	Mixed gears (hand-line, gillnet/longline combination)	2
OT1	Other (trolling, gillnet, unclassified)	1
OT2	Other (trolling, gillnet, unclassified)	2

722
723

724

725 **Table 2. Negative Log likelihood values of the different selectivity sensitivity runs of the different components based on the effective sample sizes of the length**
 726 **composition data.**

727

728

Scenario Number	Description	Log Likelihood	Survey LL	Length Comp -LL	No. of parameters estimated
Scenario 1	Base case	4257	304	4005	207
Scenario 2	Logistic LL Sel (Low Eff SS)	4316	303	4065	204
Scenario 3	Time varying Sel-LL (Low Eff SS)	4126	289	3877	223
Scenario 4	Time Varying LL and PSLs Fishery (Low Eff SS)	4112	288	3863	235
Scenario 5	Base case (higher eff SS)	21737	709	21003	207
Scenario 6	Logistic LL Sel (High Eff SS)	22149	730	21377	204
Scenario 7	Time varying Sel-LL (High Eff SS)	20940	524	20940	223
Scenario 8	Time varying Sel-LL & PS(High Eff SS)	20777	522	20201	235
Scenario 9	Aggregated Fishery Model	3866	882	2502	52

729

730

Table 3. Maximum Posterior Density (MPD) estimates from the final set of model options and associated model sensitivities. The preferred (reference) model option is highlighted.

Scenario	Selectivity Sensitivity Run	SB_0	SB_{MSY}	SB_{2011}	SB_{2011}/SB_0	SB_{2011}/SB_{MSY}	F_{2011}/F_{MSY}	MSY
1	Base case	1606040	446970	606830.3	0.38	1.36	0.31	179370
2	Logistic LL Sel (Low Eff SS)	1455880	409173	534456	0.37	1.31	0.35	163248
3	Time varying Sel-LL (Low Eff SS)	2493330	705780	1622145	0.65	2.30	0.14	273752
4	LL and PLS Fishery (Low Eff SS)	2432020	696212	1598100	0.66	2.30	0.15	259886
5	Base case (higher eff SS)	1082610	300837	343326.8	0.32	1.14	0.51	114591
6	Logistic LL Sel (High Eff SS)	1323390	243942	343327	0.26	1.41	0.66	93973
7	Time varying Sel-LL (High Eff SS)	948687	270865	525487	0.55	1.94	0.39	106121
8	Time varying Sel-LL & PS(High Eff SS)	929923	268817	528458	0.57	1.97	0.41	96629
9	Aggregated Fisheries	938225	165640	421377	0.45	2.54	0.24	193240

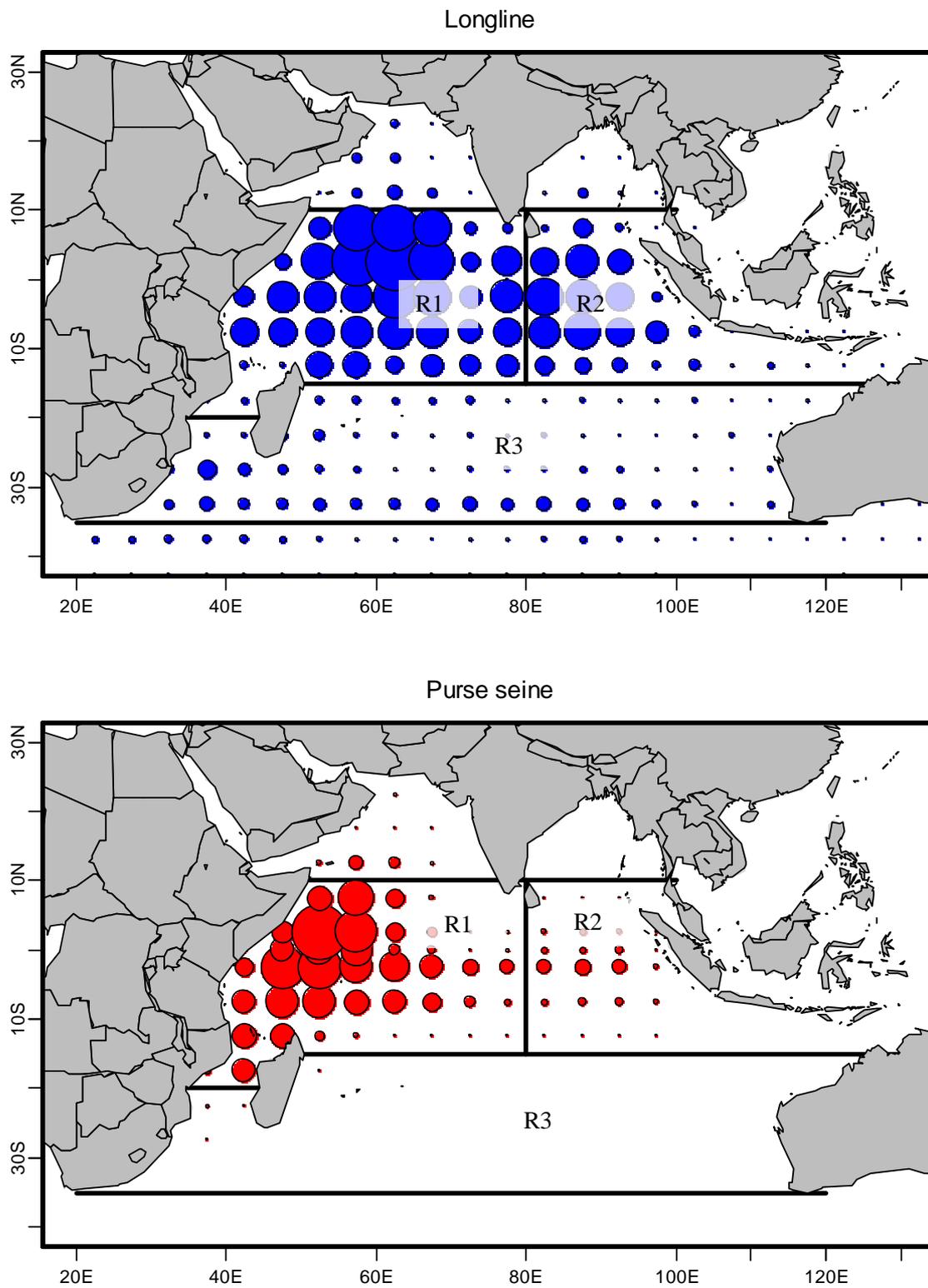


Figure 1. Aggregate LL and PS catch (max bet catch in 5 deg cell aggregated over time 70159.62 mt)

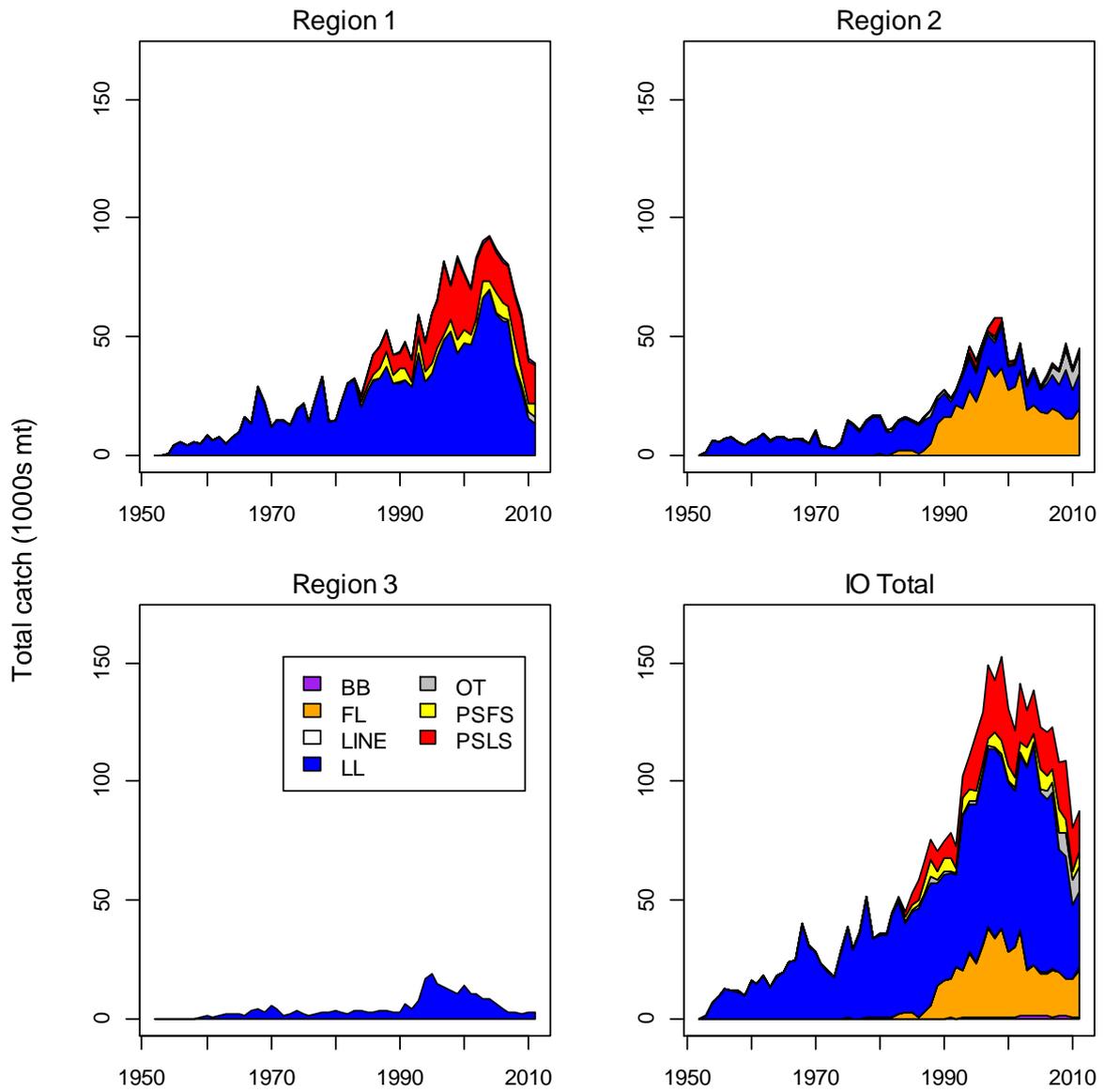


Figure 2. Annual catches by fishery and region.

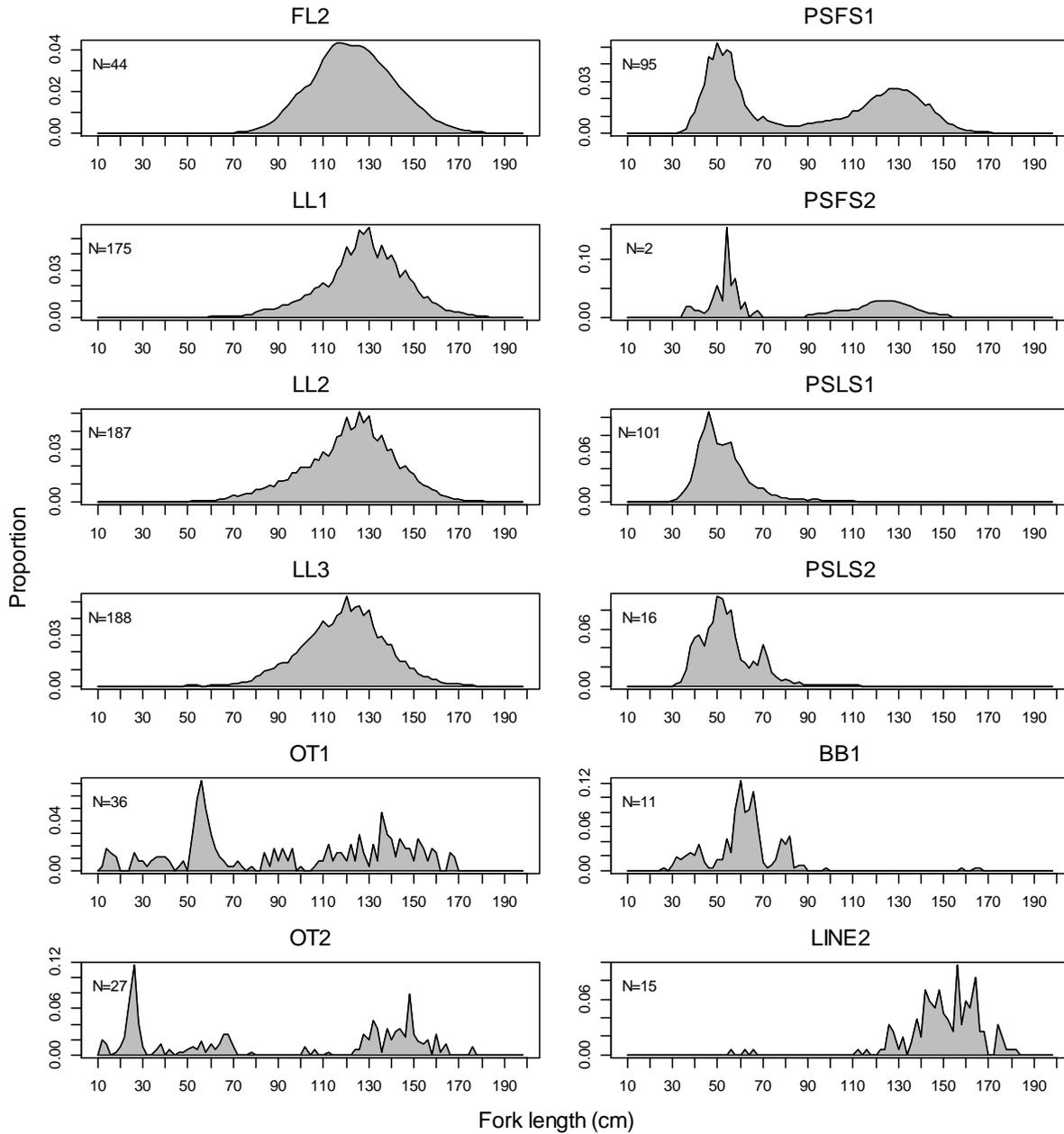


Figure 3. Length compositions of bigeye tuna samples aggregated by fishery. N represents the number of quarterly samples.

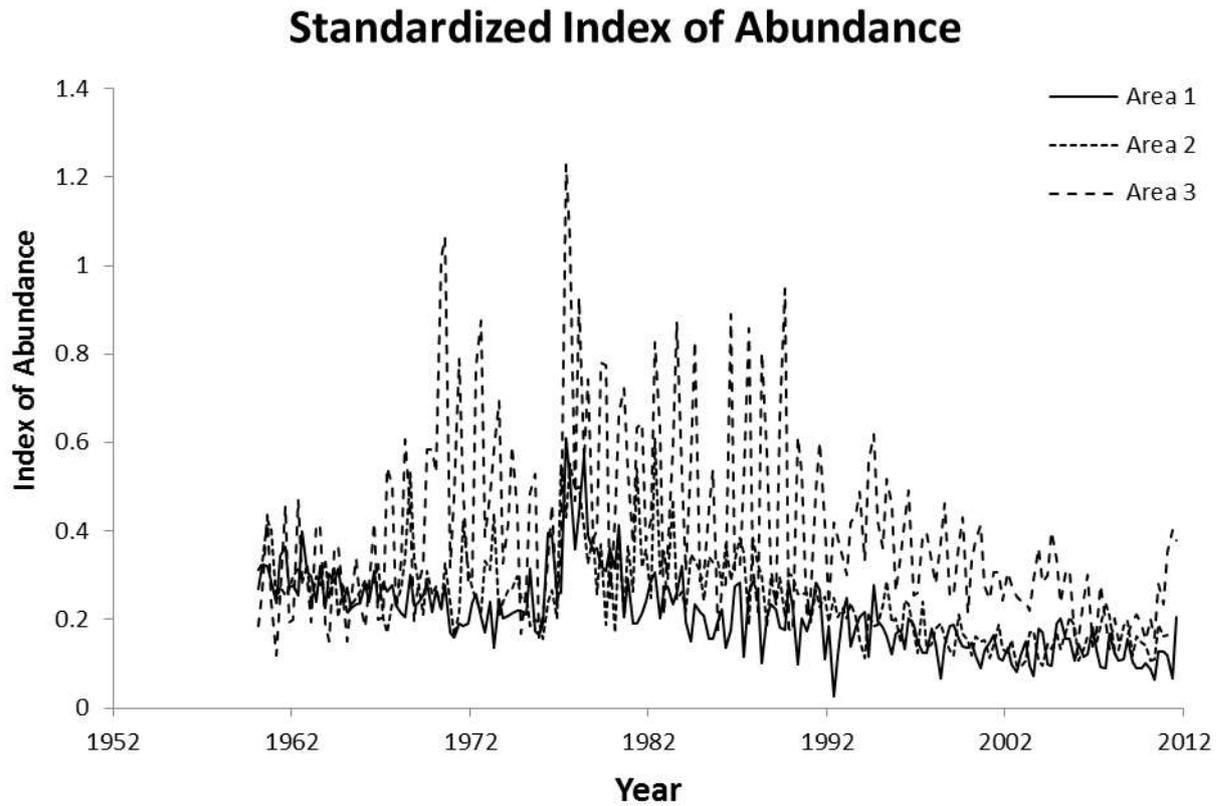


Figure 4. Standardised longline CPUE indices for each region. The longline series are standardised among regions

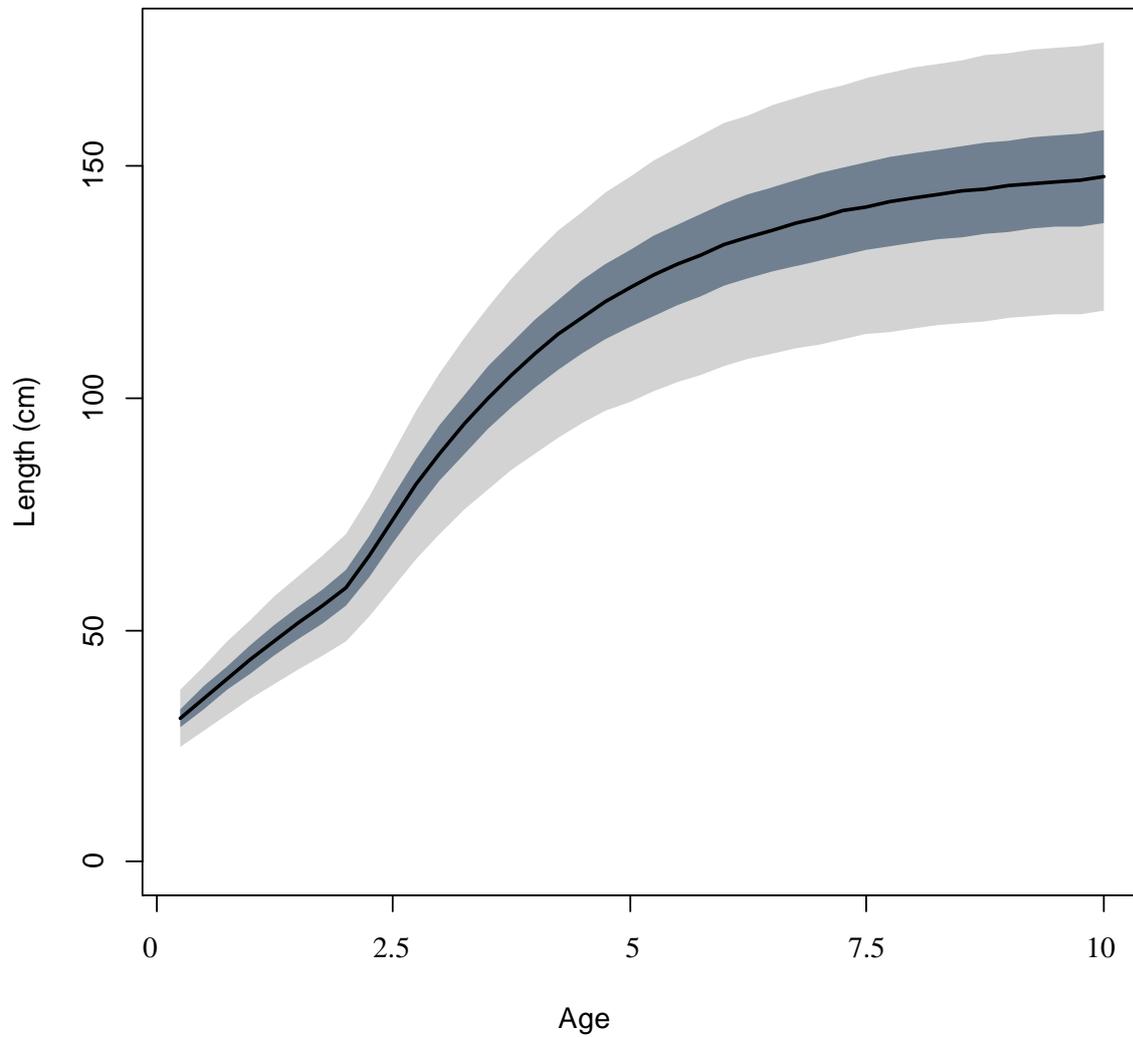


Figure 5. Growth of Indian Ocean bigeye tuna (following Everson et al 2012). The dark grey region represents the quartile range of the distribution of length-at-age and the light grey region represents the 95% confidence interval.

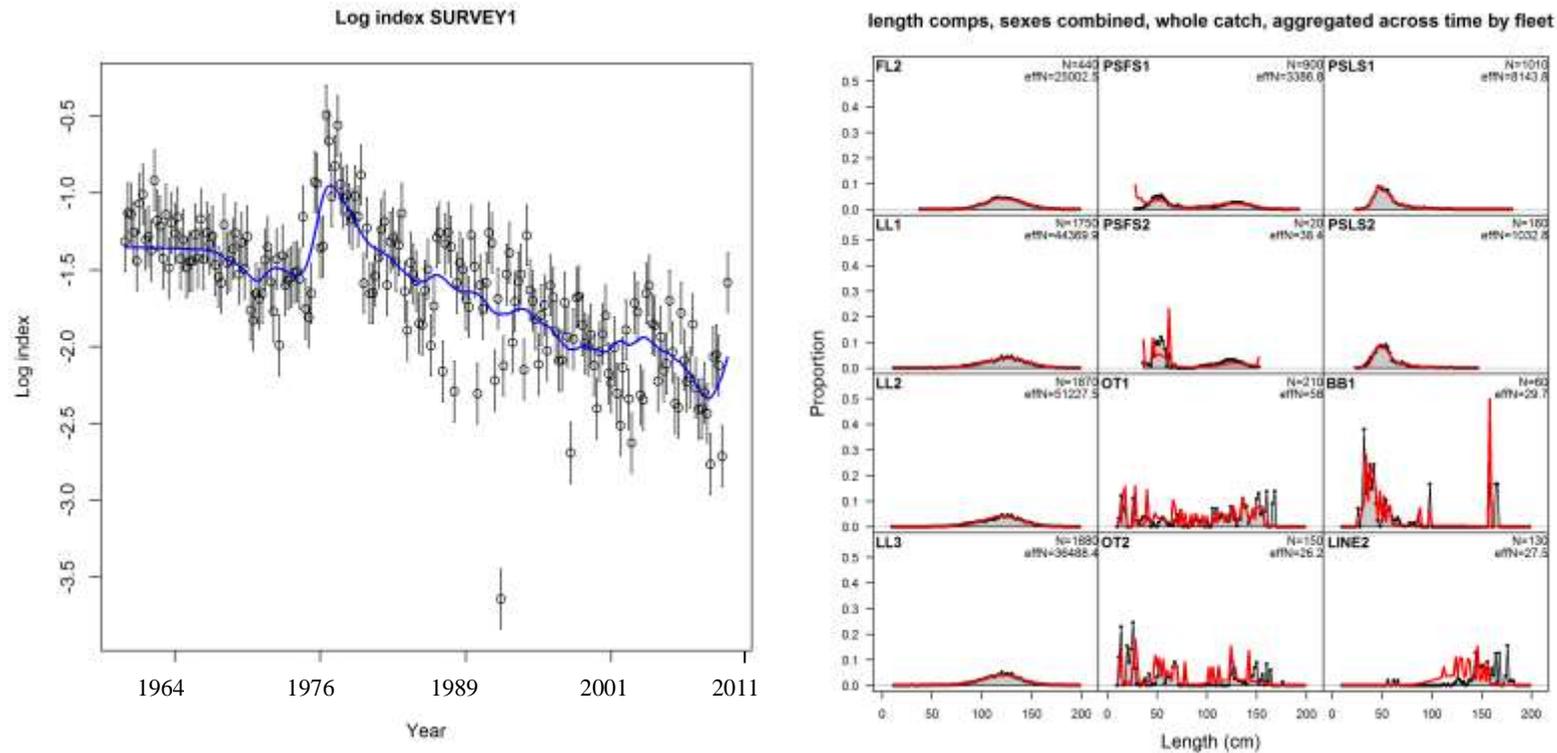


Figure 6. Fit of the base model the index of abundance as obtained from the Japanese logline fishery and the average length composition from the data aggregated across time by each fishery separately

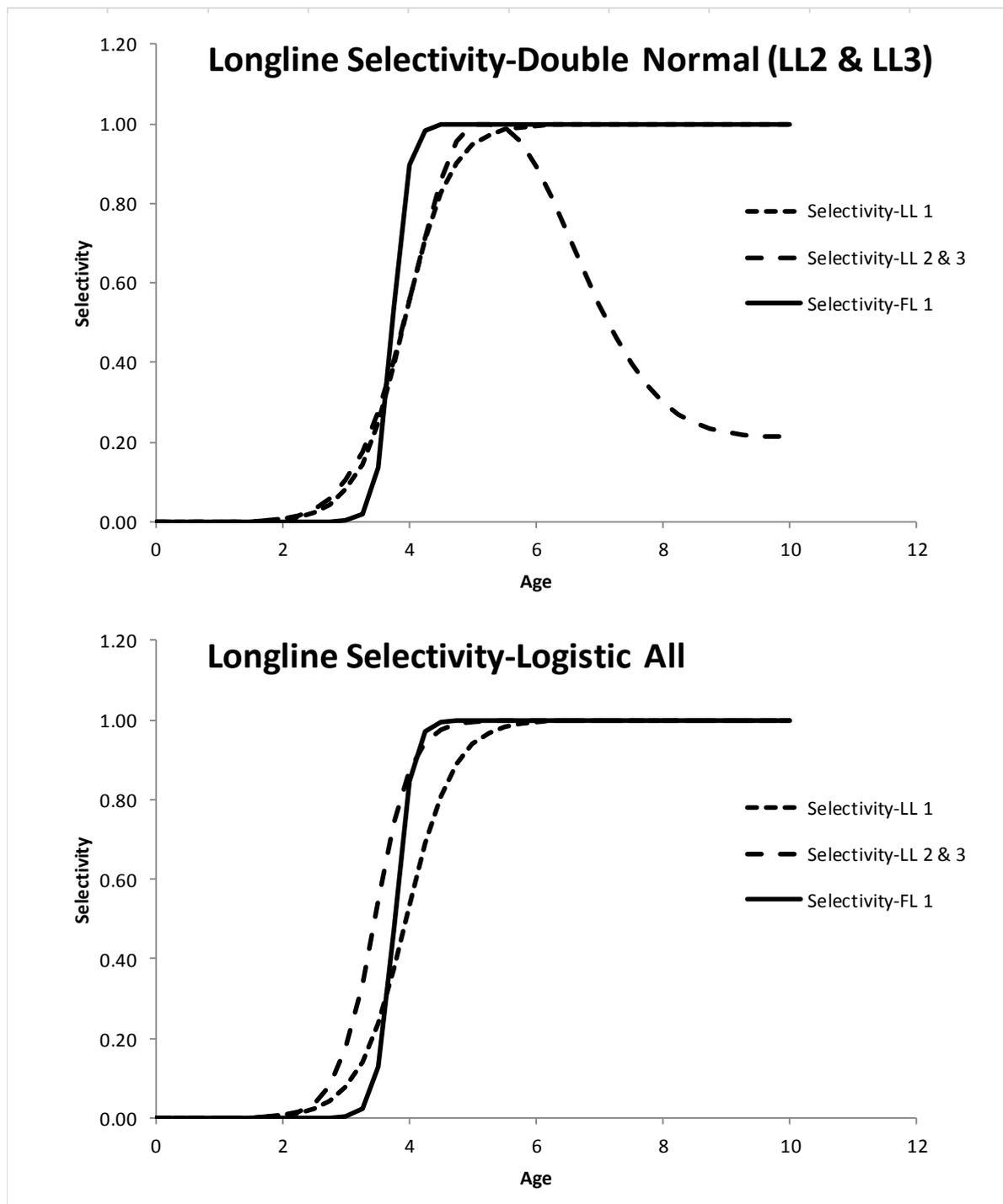


Figure 7. Logistic versus Double Normal Selectivity estimated in LL and Fresh Tuna (FL) fisheries in area 1, 2 and 3. Note LL 2 and 3 selectivity is modelled identically.

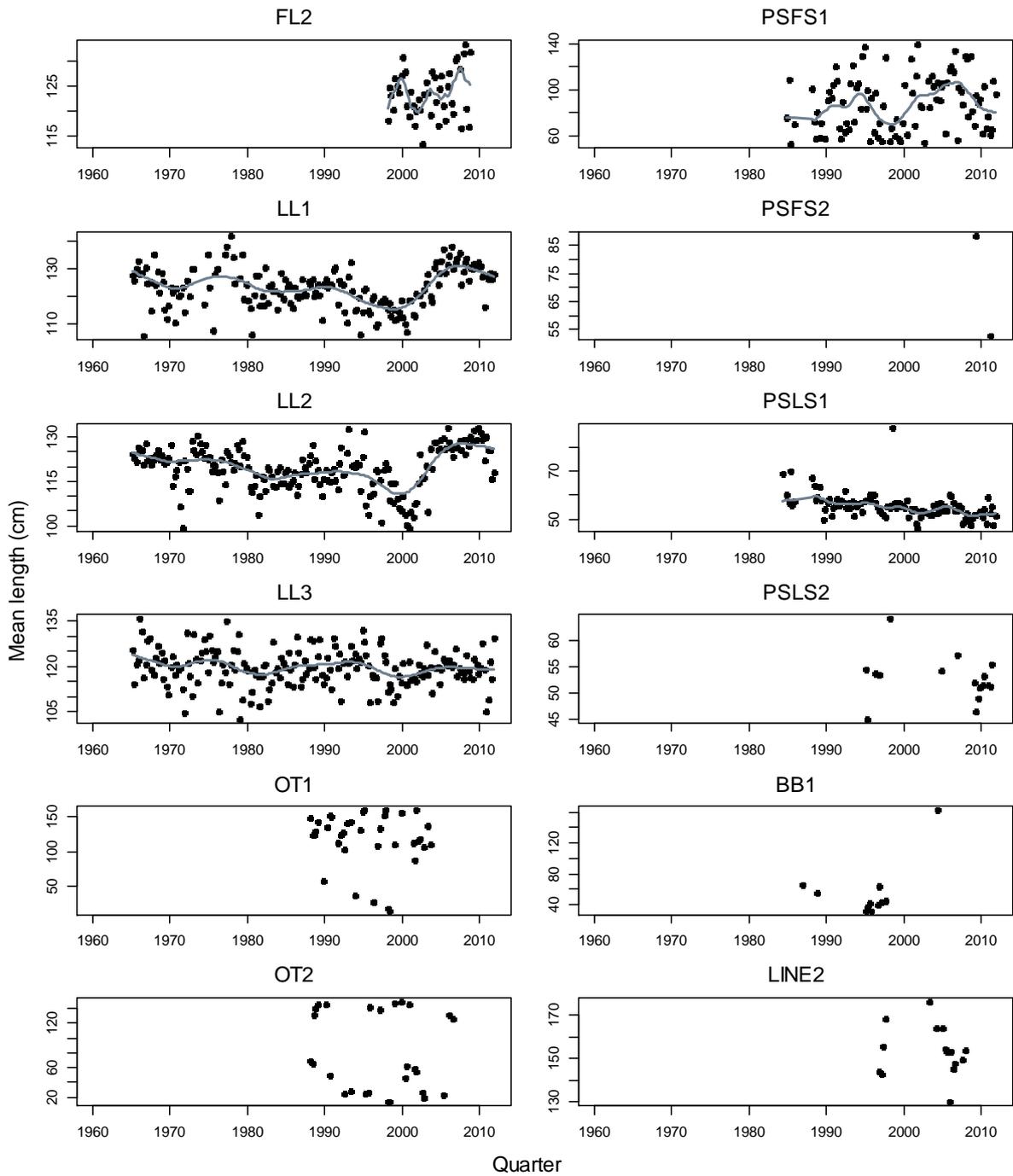


Figure 8. The average length (fork length, cm) of bigeye in the individual samples from each fishery. The grey line represents a lowess smoothed trend. The y-axis differs among the individual plots.

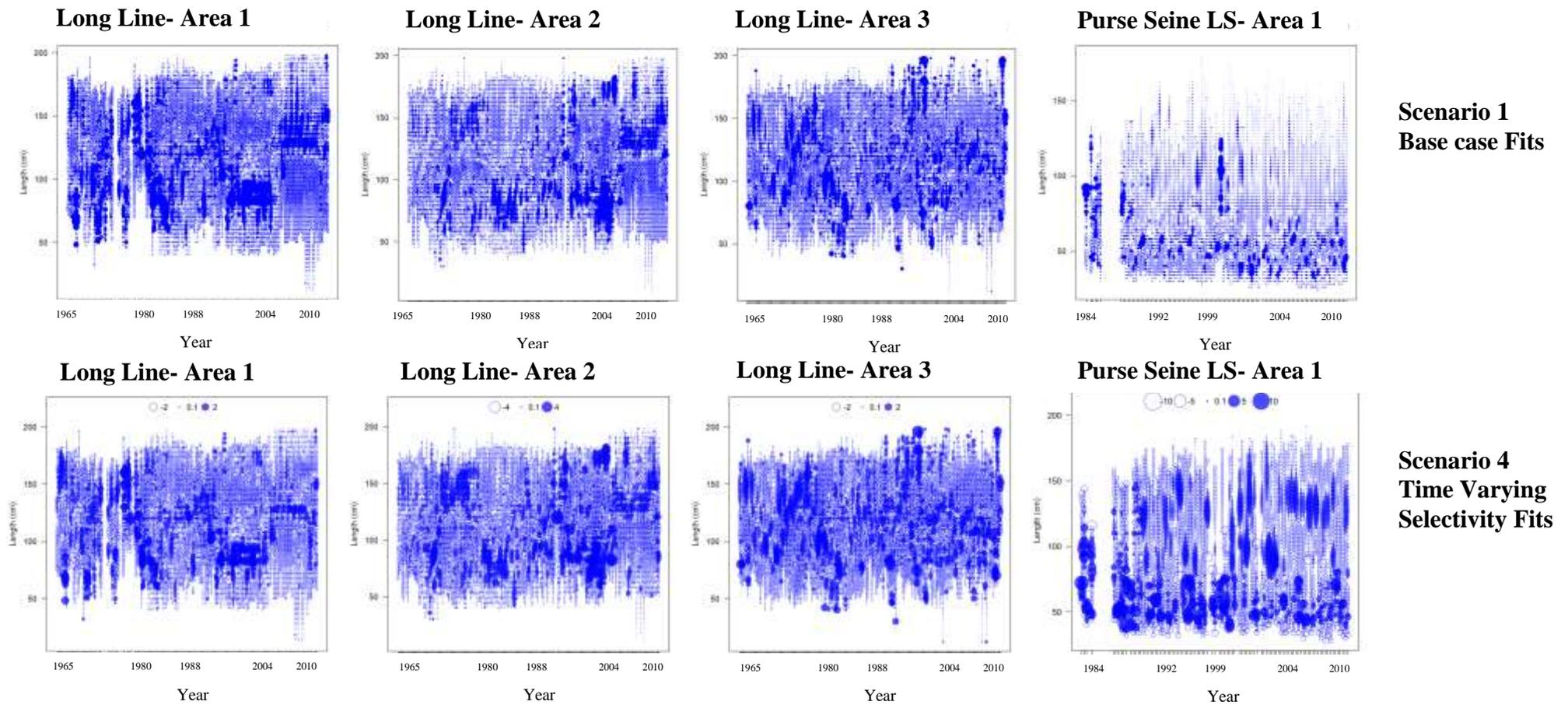


Figure 9: Marginal improvements in Pearson's residuals for length composition data FL2, LL 2 and PSFS 1 when fitting time varying selectivity in all the LL and PS fisheries by the blocks 1952- 1971, 1972-2001, and 2002-2011 respectively

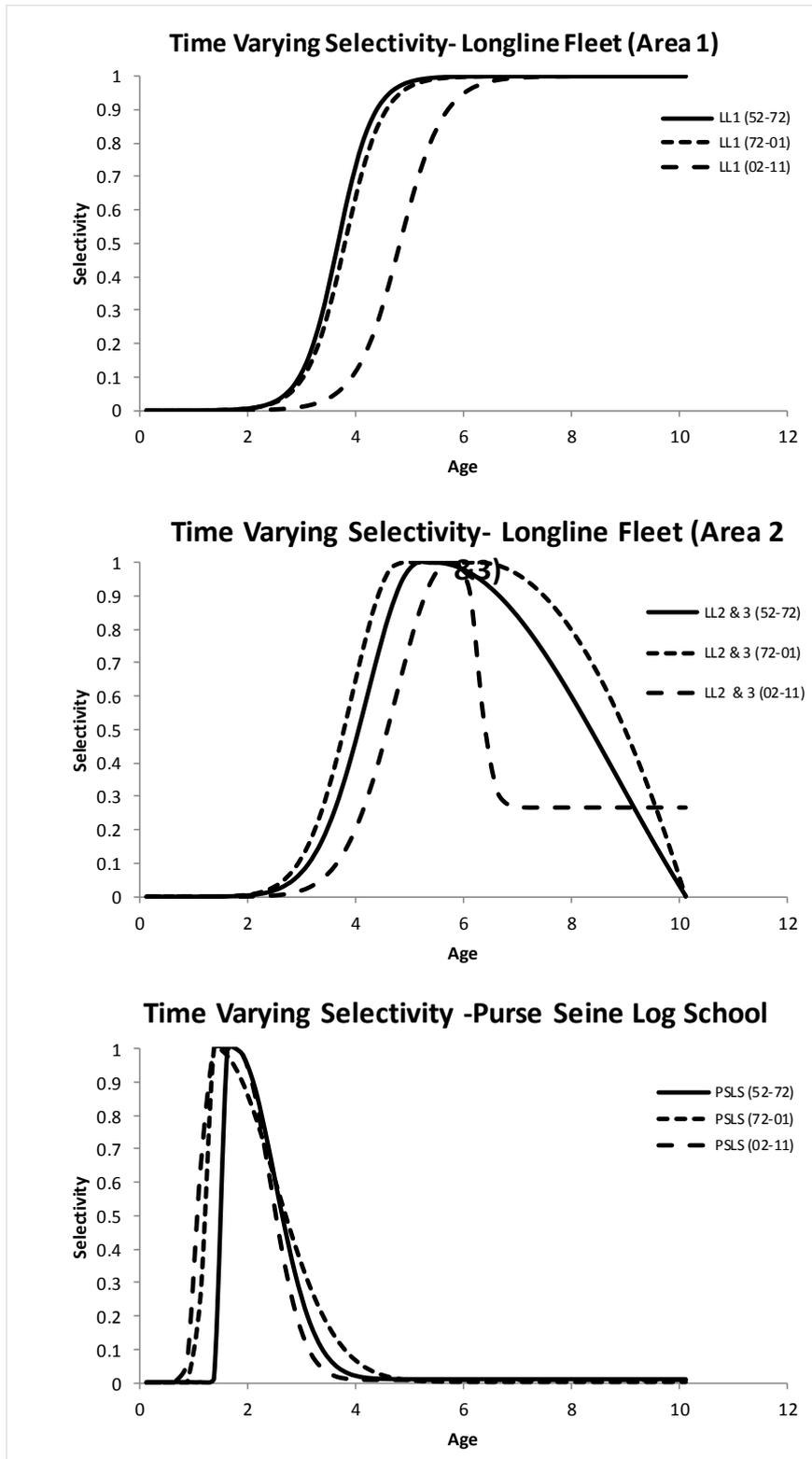


Figure 10: Time Varying selectivity using higher Effective Samples sizes (200), between the Longline and Purse Seine fisheries using the time blocks 1952- 1971, 1972-2001, and 2002-2011 respectively.

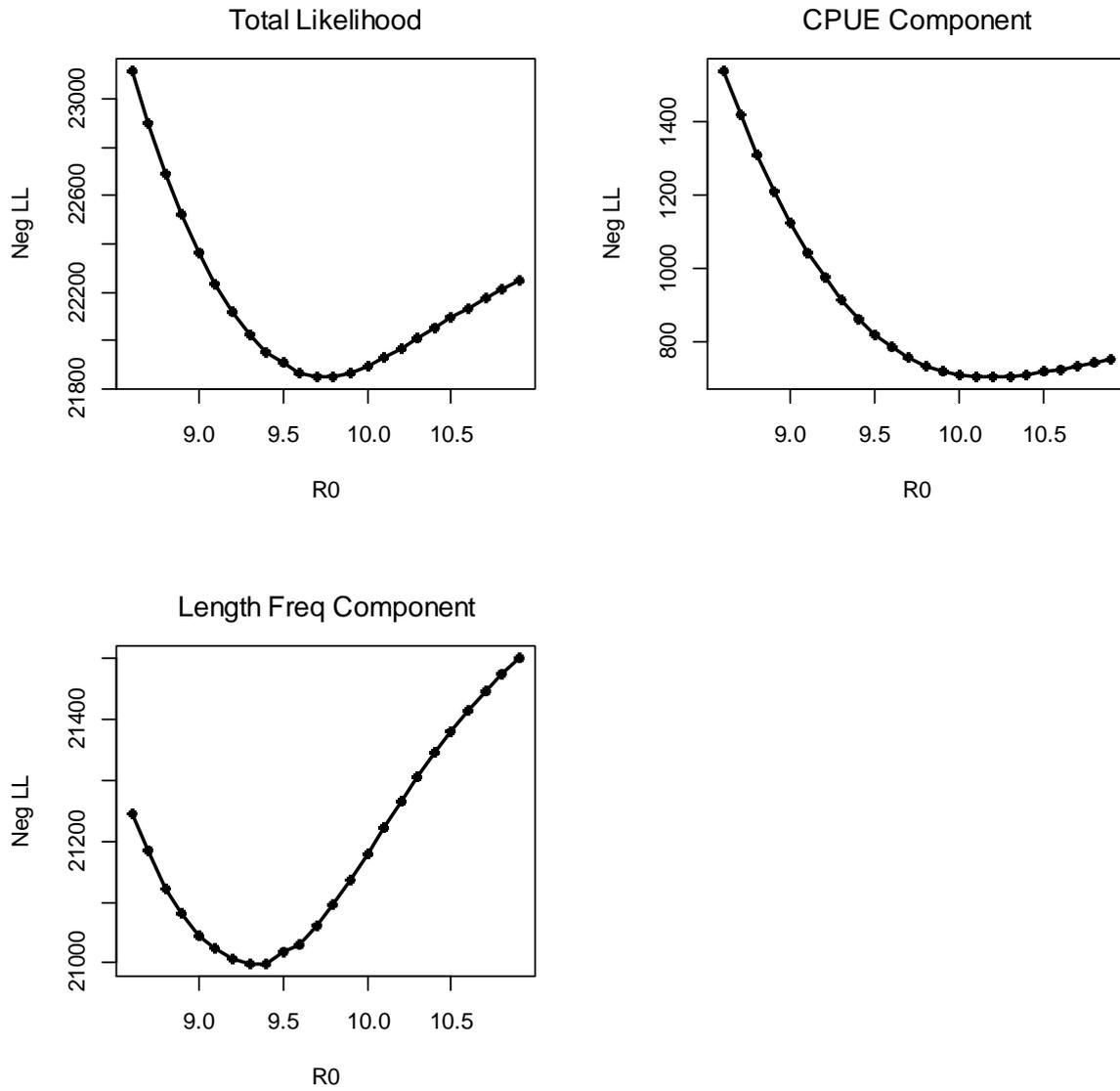


Figure 11: Likelihood profile for the R_0 parameter for the single region model. The likelihood profiles for the CPUE and length frequency components of the total likelihood are also presented.

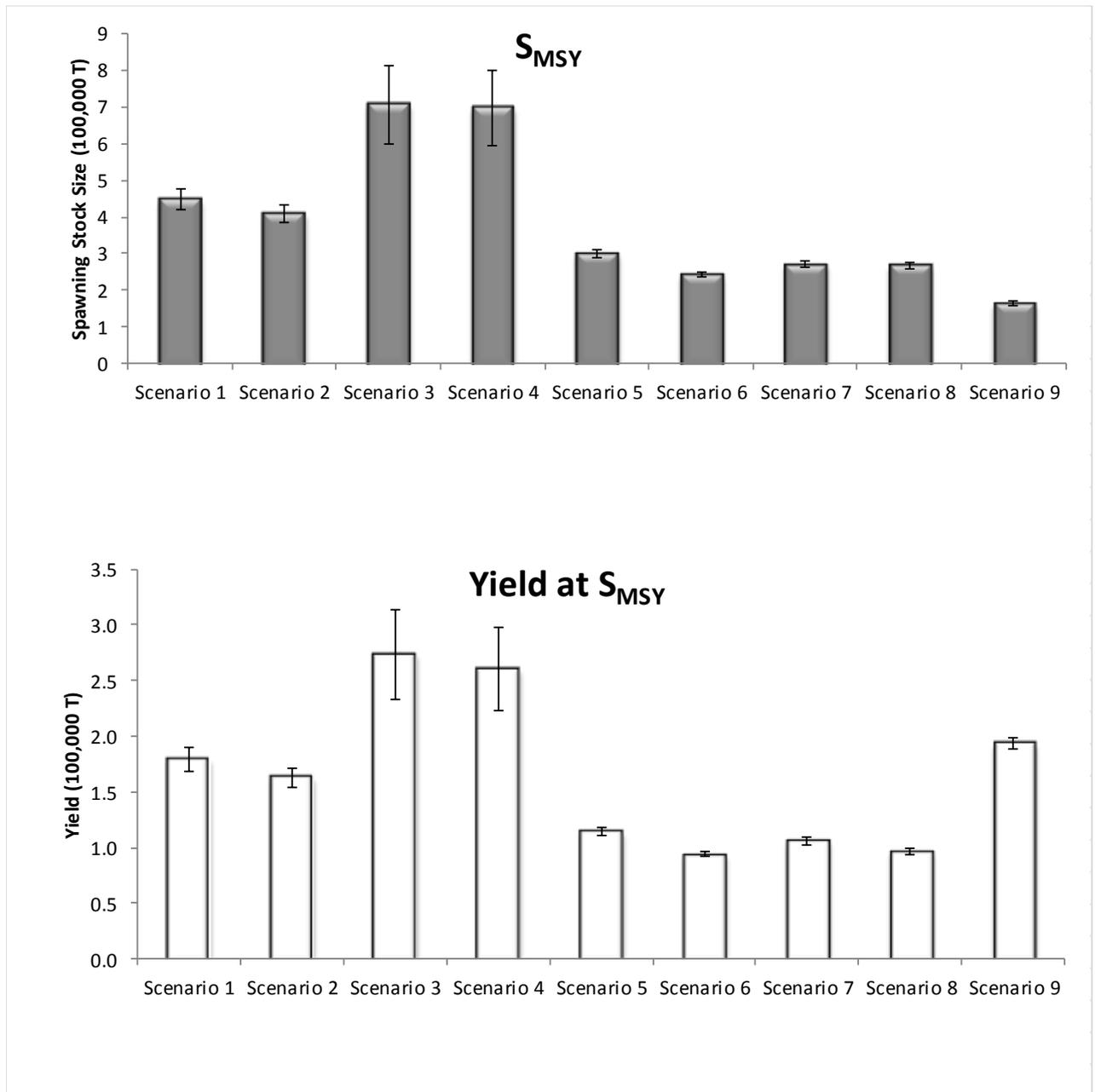


Figure 12. Target reference points as estimated by the different models summarized in Table 2 and Table 3.

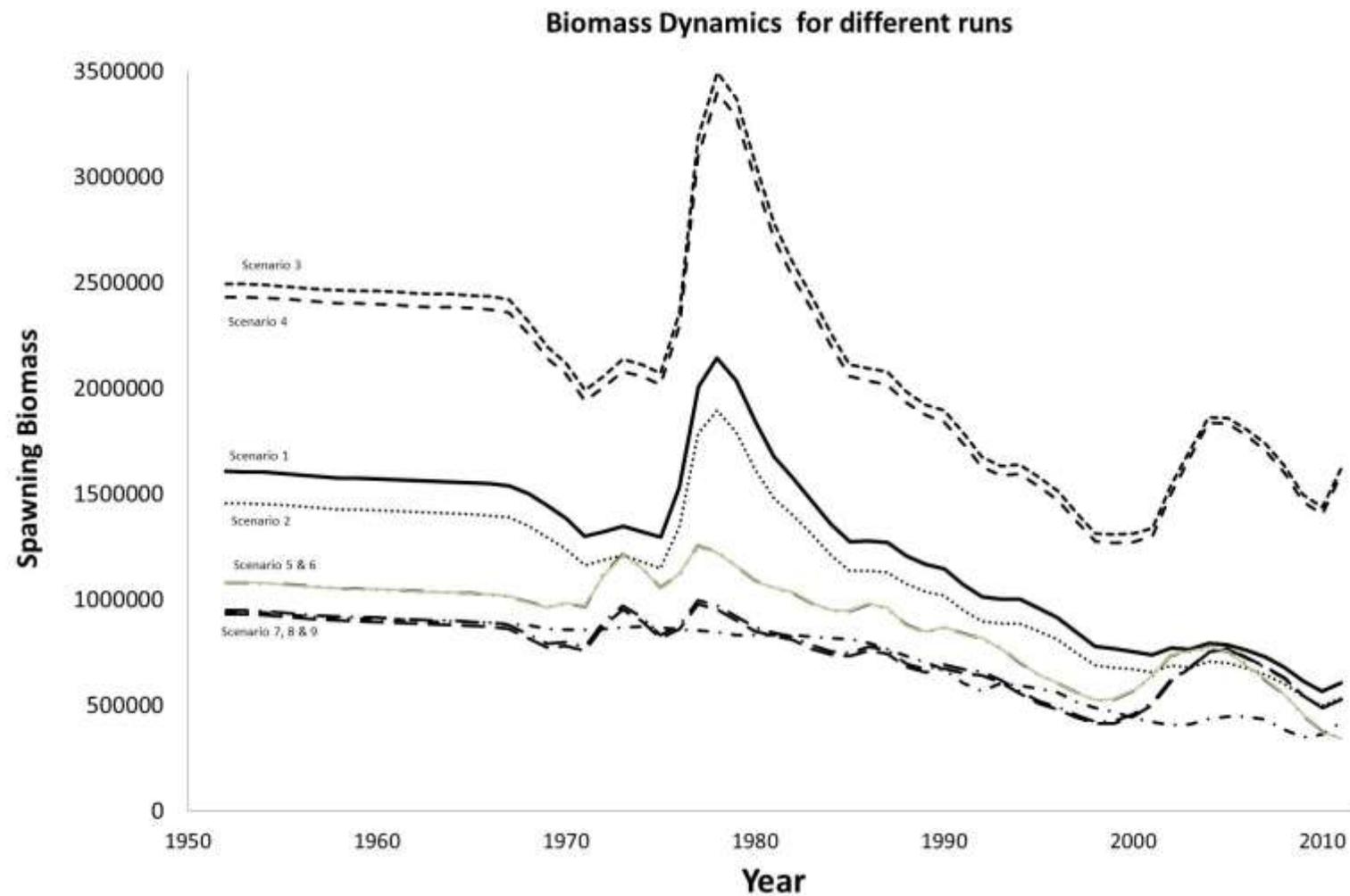


Figure 13. The different Biomass trajectories estimated from the single region models using time-varying selectivity with contrasting weighting of the length frequency data (different effective sample sizes).

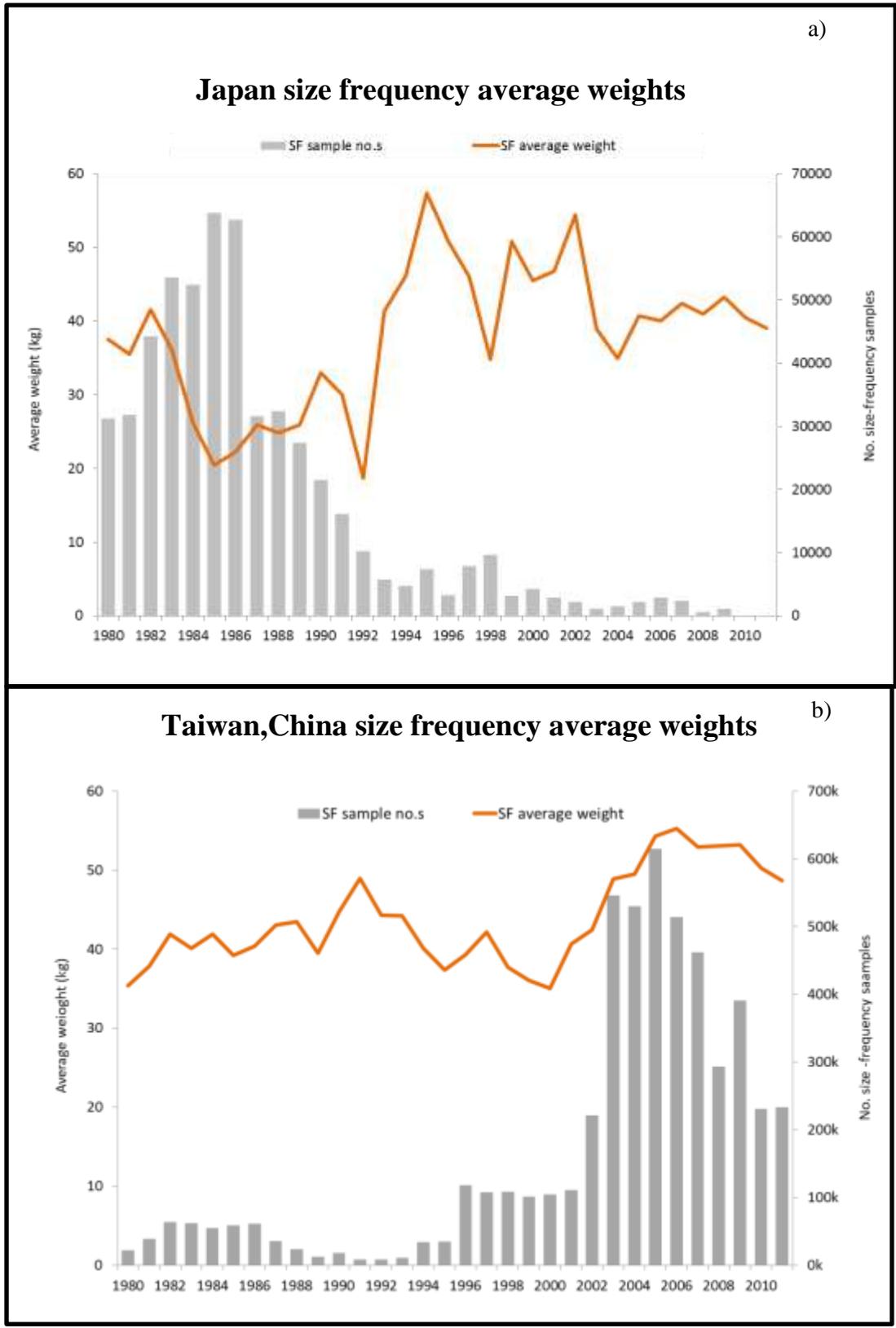


Figure 14. Length frequency data trends in average catch and sample sizes from Japan (fig. 14a) and Taiwan, China (fig. 14b) longline fleets over the time period used in the assessment.

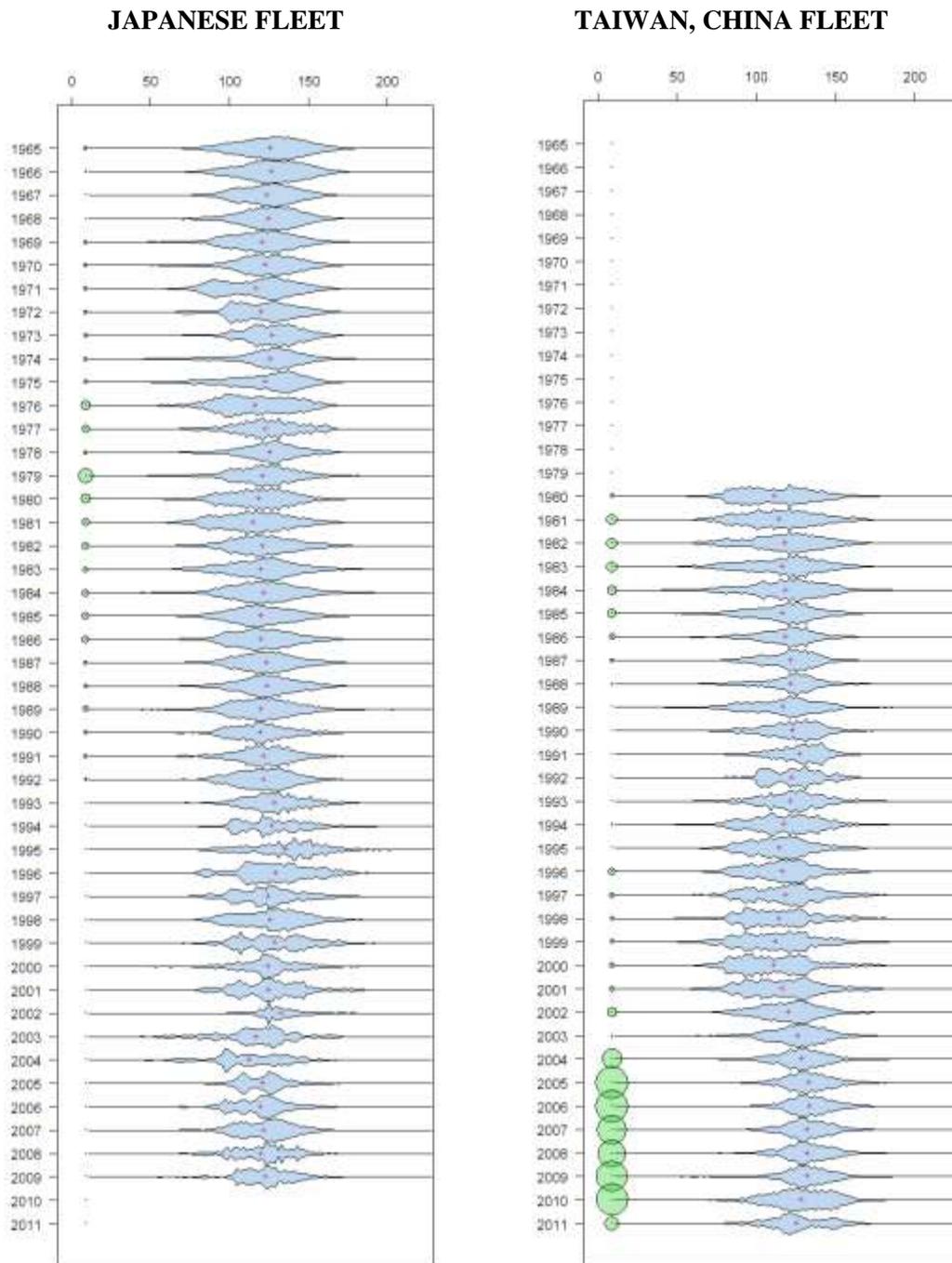


Figure 15: Comparison of BET length frequency distributions of Tawianese and Japanese Longline fleets. The size of the green proportional circles indicates the sampling coverage in each year, which are scaled relative to the minimum sampling coverage of one fish per tonne of catch recommended by the Indian Ocean Tuna Commission (denoted by the black circle at the centre of each proportional circle). Years with proportional circles larger than the minimum sampling standard indicate relatively high sampling coverage in a given year; the larger the circle the higher the sampling coverage. The crosshairs indicate the average length of sampled cohorts in each year class.