

# A Length-Based Catch Curve for Multigear Fisheries

IO YFT Example

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# Motivation

- Use length frequency data (as LBSPR with variable growth)
- Bayesian fitting
- Allow flexible selectivity functions and multiple gears

# Assumptions

- 1. The population has been in an approximate steady-state for a generation or more around when the length sampling takes place (No time series).**
2. Mean growth follows the von Bertalanffy growth curve.
3. Fish asymptotic size ( $L_{\infty}$ ) is Gamma distributed for individual fish which governs growth variability.
4. Mortality fixed within each length interval. It can vary arbitrarily between intervals.
- 5. Length data are representative of the catch length composition and the relative total catch numbers for each selectivity group.**

# **MODEL DESCRIPTION**

# Population Model

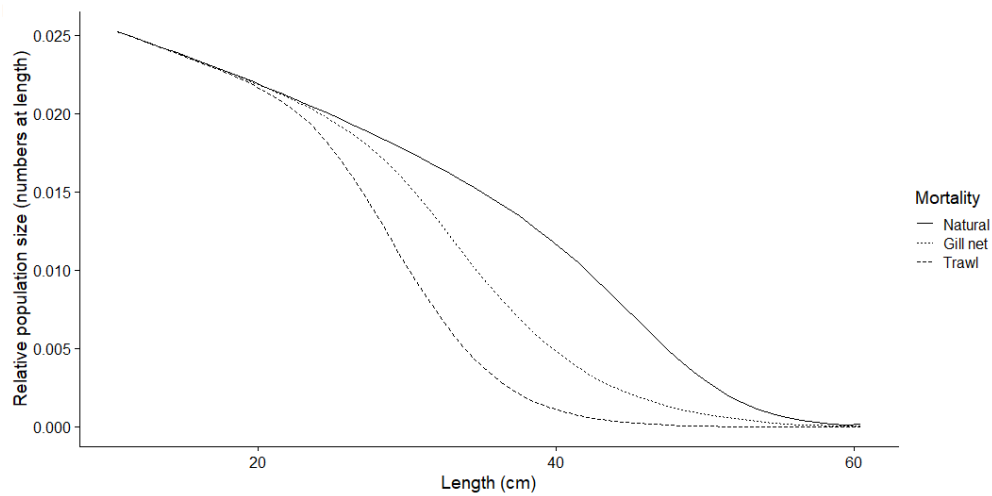
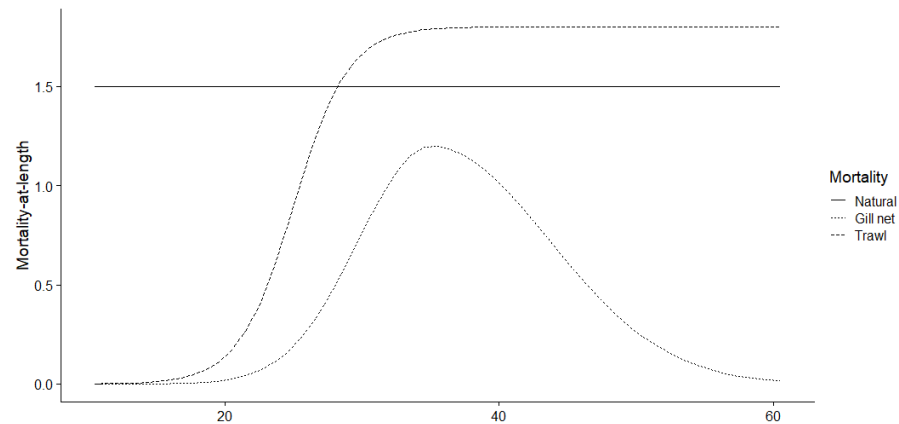
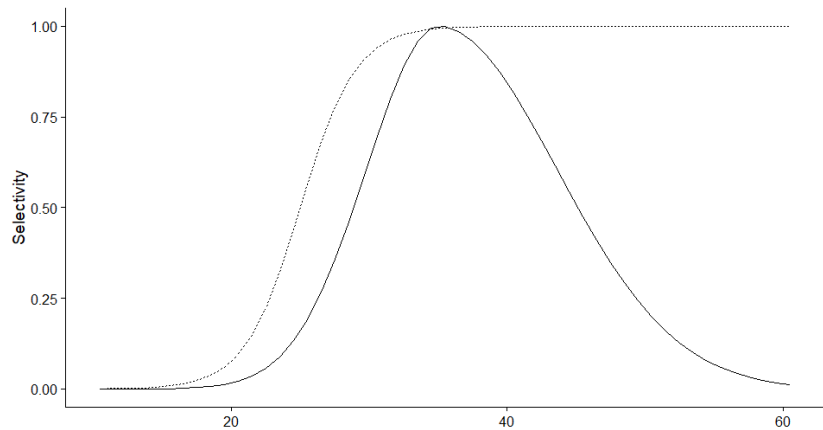
The probability that fish will survive to length interval  $n$  with lower bound  $L_n$  is given by:

$$S_n = \int_{L_n}^{\infty} \frac{\beta^\alpha}{\Gamma(\alpha)} L_\infty^{\alpha-1} e^{-\beta L_\infty} (L_\infty - L_0)^{-Z_1} (L_\infty - L_n)^{Z_n} \prod_{i=1}^{n-1} (L_\infty - L_i)^{Z_i - Z_{i+1}} dL_\infty$$

- $N_n = \frac{S_n - S_{n+1}}{Z_n}$
- $C_n = \frac{F_n}{Z_n} (S_n - S_{n+1})$
- $F_n$  will reflect the selectivity pattern, can be split into multiple gears.

Gauss-Laguerre quadrature is used for numerical integration (fast and accurate in this case).

# Multiple Gears



**APPLICATION**

# Application R package: *fishblicc*

- Work-In-Progress
- Implements Bayesian length-based catch curve (in Stan)
- Selectivity models based on **simple mixtures** of logistic, normal, single-sided normal and double-sided normal
- Simulation testing suggests similar results to LBSPR for single gear logistic selectivity
- R Package: <https://github.com/PaulAHMedley/fishblicc>

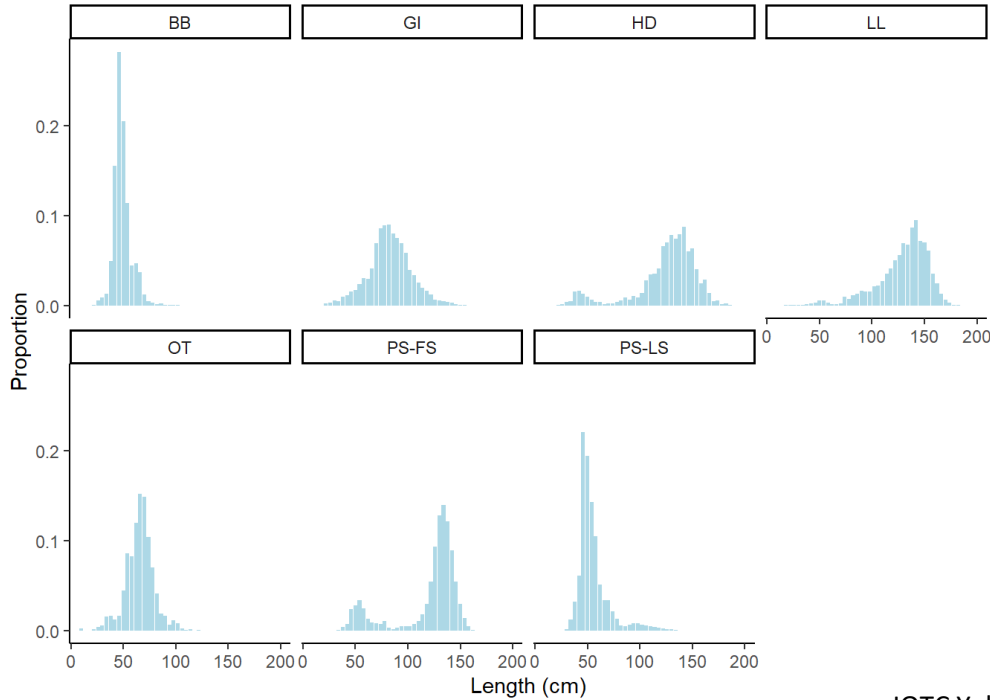


# Priors

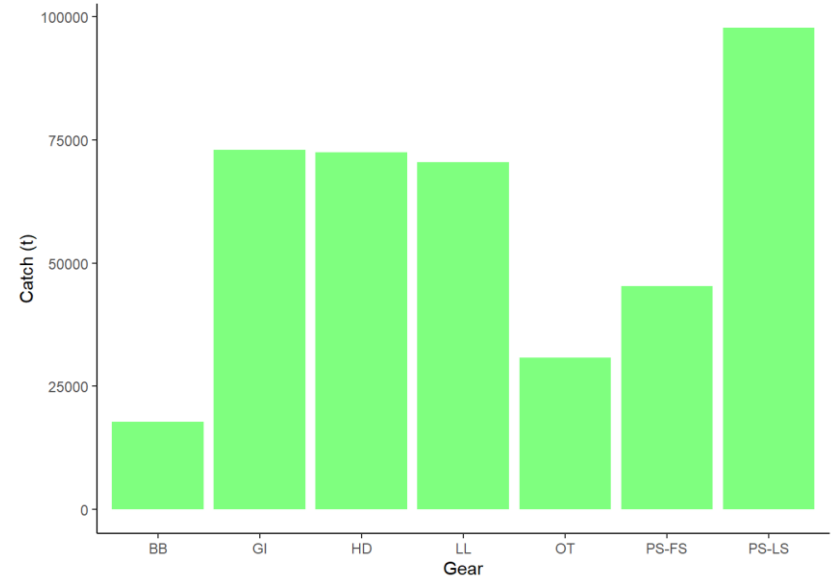
- Informative priors:
  - $L_\infty$  is required - often available from Fishbase or elsewhere
  - Natural mortality:  $M \approx 1.5 K$
  - Growth CV ( $G_{\text{alpha}}$ ) - default 10%
  - $K$  and  $t_0$  not required
- Non-informative priors (usually)
  - Fishing mortality / selectivity parameters
  - Observation error

**ILLUSTRATIVE EXAMPLE: IO YELLOWFIN**

# Yellowfin Length Frequency Data + Catches

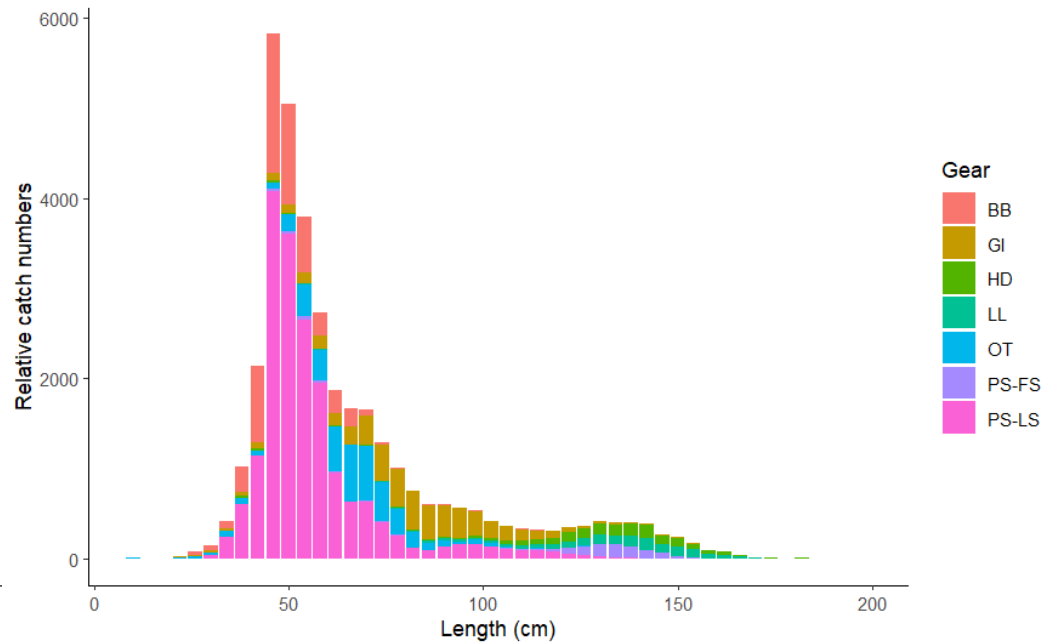
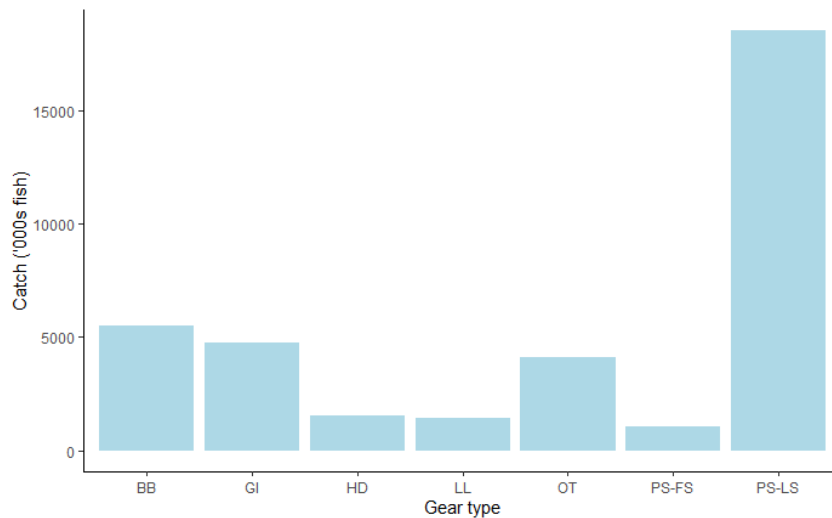


Aggregated 2014 – 2018

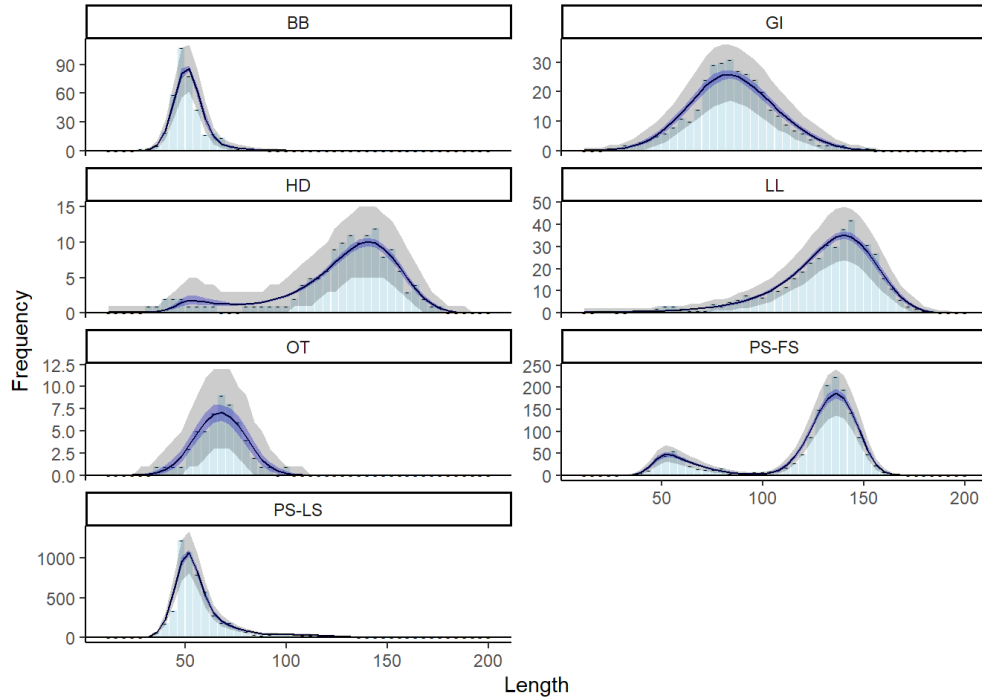


IOTC Yellowfin data used in the 2019 stock assessment SS3 V3.30  
[https://iotc.org/sites/default/files/documents/2019/09/IOTC-2019-WPTT21-DATA15-YFT\\_SA\\_0.zip#\"Stock assessment inputs \(SS3 and SCAA\) for YFT\"#\"IOTC-2019-WPTT21-DATA15\"](https://iotc.org/sites/default/files/documents/2019/09/IOTC-2019-WPTT21-DATA15-YFT_SA_0.zip#\)

# Catch Numbers

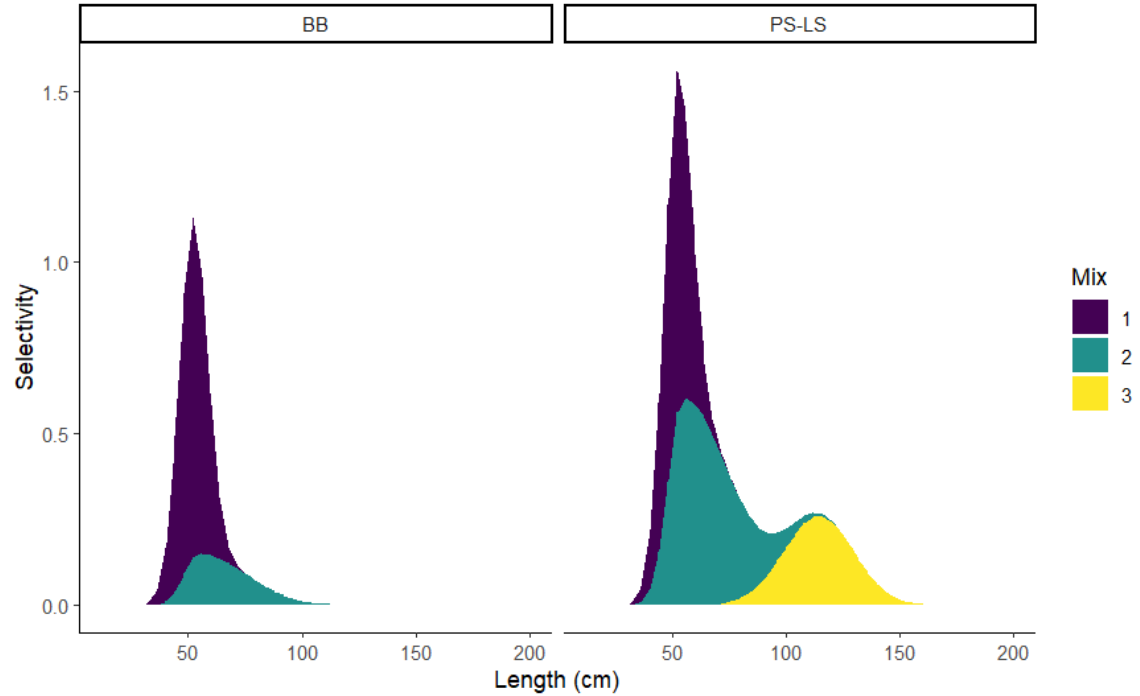


# Fitted model



- Selectivity mixtures
- Length-inverse M
- Fishbase  $L_{\infty}$

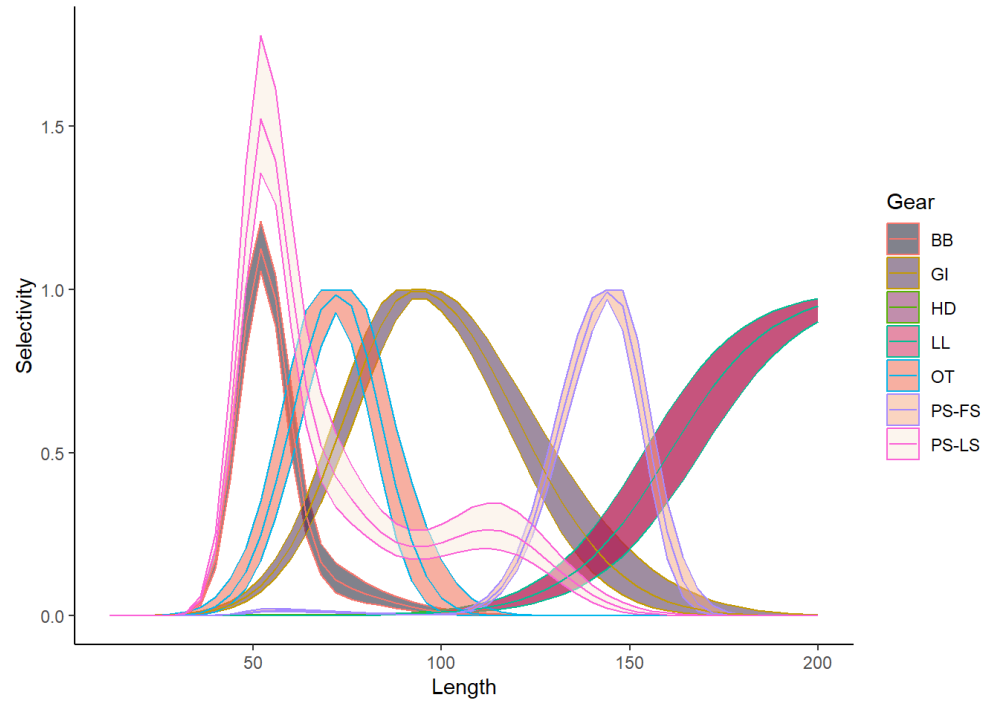
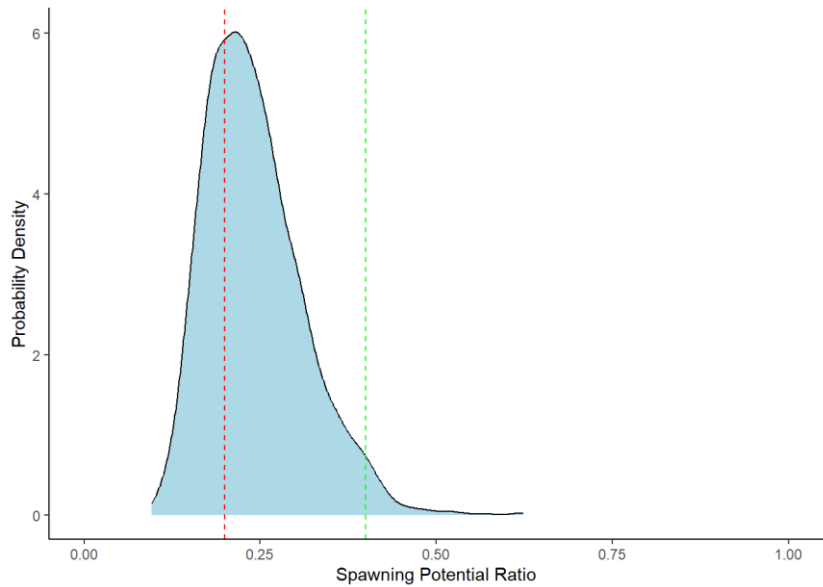
# Selectivity Mixtures



# Model Flexibility

Scenario	$L_{\infty}$	Galpha	M/K	SPR	Ip	Decision
All domed single selectivity	166.67	73.17	4.00	0.80	-812.9	Rejected
Selectivity Mixture Model	179.06	133.28	1.61	0.21	-550.7	Accept
Allow Linf estimation	160.44	170.07	1.50	0.61	-549.6	Sensitivity
Length-inverse M	178.87	123.84	1.68	0.23	-547.6	Accept
Longline dome-shaped	184.30	98.14	1.48	0.80	-559.3	Rejected
SS3 parameters	148.16	164.54	0.73	0.48	-537.1	Sensitivity

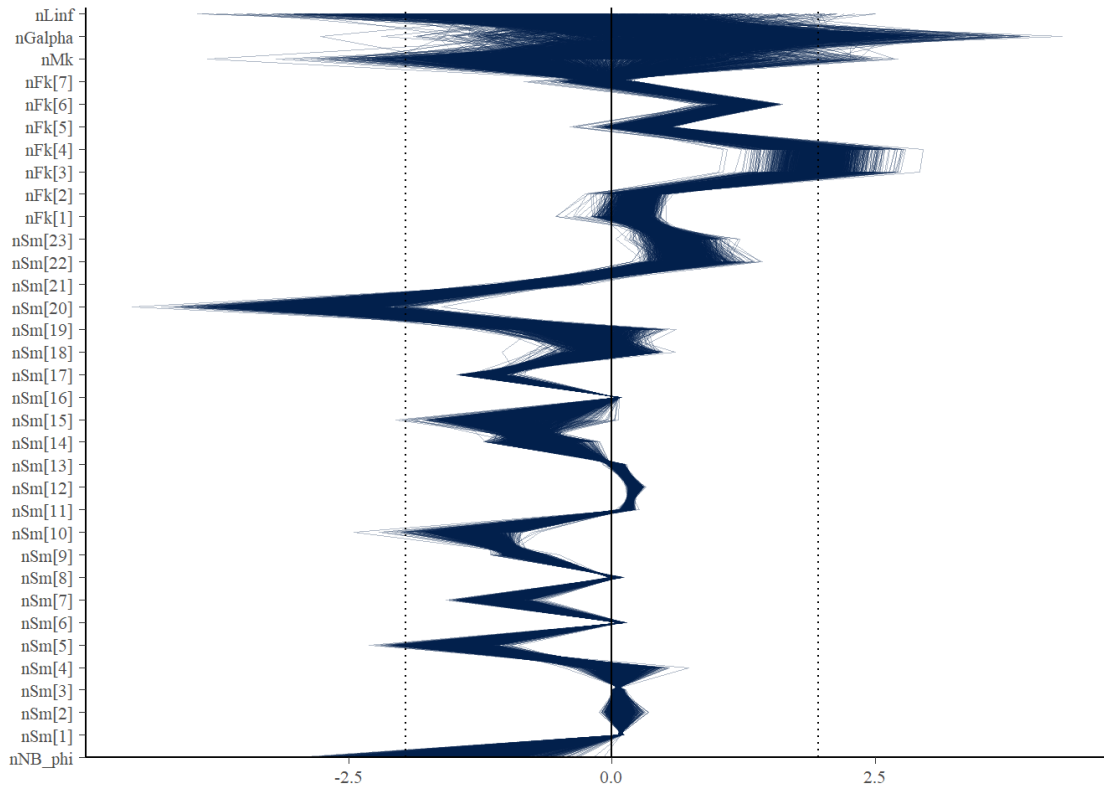
# Results



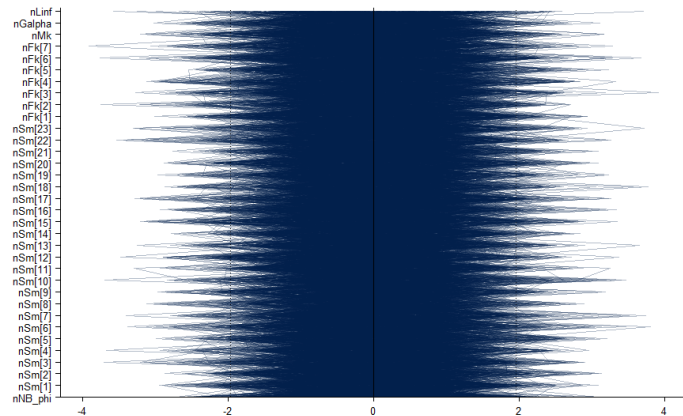


# Parameter Estimates

## Posterior



## Prior



# Conclusion

- Bayesian length-based catch curve with flexible modelling of mortality-at-length implemented in the *fishblicc* package
- *Key assumption* is population is in stationary state
- *Fits* single and multiple sample length frequency data
- *Estimates* F-at-length, selectivity, SPR, YPR etc.
- *Used* for data limited assessments + examine selectivity models
- *Caution* with overfitting (use sensitivities)